

1 Evaluation of Chinese Quad-polarization Gaofen-3 SAR Wave 2 Mode Data for Significant Wave Height Retrieval

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17 **Abstract**

18
19 Our work describes the accuracy of the Chinese quad-polarization Gaofen-3 (GF-3)
20 synthetic aperture radar (SAR) wave mode data for wave retrieval and provides
21 guidance for operational applications of GF-3 SAR. In this study, we have evaluated
22 the accuracy of SAR-derived significant wave height (SWH) from 10514 GF-3 SAR
23 images with visible wave streak acquired in wave mode by using the existing wave
24 retrieval algorithms, e.g., the theoretical-based algorithm parameterized first-guess
25 spectrum method (PFSM), the empirical algorithm CSAR_WAVE2 for
26 VV-polarization, and the algorithm for quad-polarization (Q-P). The retrieved SWHs
27 are compared with the European Centre for Medium-Range Weather Forecasts
28 (ECMWF) reanalysis field at 0.125° grids. The root mean square error (RMSE) of
29 SWH is 0.57m by using CSAR_WAVE2 is achieved, which is less than the analysis
30 results achieved by using algorithm PFSM and Q-P. The statistical analysis also
31 indicates that wind speed has little impact on bias with increasing wind speed.
32 However, the retrieval tends to overestimate when SWH is smaller than 2.5m and

33 underestimate with increasing SWH. Moreover, the retrieval error grows with
34 decreasing SWH at low state. This kind of behaviour gives a perspective of the
35 improvement of SWH retrieval algorithm for GF-3 SAR acquired in wave mode.

36 **1. Introduction**

37 Gaofen-3 was launched by the China Academy of Space Technology (CAST) on
38 August 2016 and is the first Chinese civilian satellite for scientific research, to carry
39 synthetic aperture radar (SAR) at C-band as well as Canadian Radarsat-2 (R-2) and
40 European Sentinel-1 (S-1). The National Ocean Satellite Application Center (NSOAS)
41 is responsible for marine applications of GF-3 SAR. Through cooperation projects
42 with NSOAS, some researchers have made a preliminary analysis of wind (Wang et al.
43 2017; Ren et al. 2017) and wave (Shao et al. 2017) retrieval from GF-3 SAR acquired
44 in imaging mode, e.g., standard stripmap (SS) and quad-polarization mode (QPS-I/II)
45 (vertical-vertical (VV); vertical-horizontal (VH); horizontal-horizontal (HH) and
46 horizontal-vertical (HV)). In addition, the feasibility of retrieving sea surface wind
47 speeds from VH-polarization GF-3 SAR acquired in global observation (GLO) and
48 wide scanSAR (WSC) mode data with a large spatial coverage of more than 400km
49 was recently reported in Shao et. al (2018), concluding that GF-3 SAR is a promising
50 tool for the monitoring of strong winds under typhoon conditions.

51 Algorithms for wave retrieval have been well studied over previous decades
52 (Chapron et al. 2001; Díaz-Méndez et al. 2010; Zhang et al. 2015). The algorithms
53 used can be divided into three categories. The first two kinds are the theoretical-based
54 algorithms exploited for co-polarization (VV or HH) and quad-polarization, both of
55 which are based on the wave mapping mechanism on SAR. The SAR mapping
56 mechanism includes tilt modulation (Lyzenga 1986), hydrodynamic modulation
57 (Feindt et al. 1986) and velocity bunching (Alpers et al. 1981; Alpers and Bruning
58 1986). The other is an empirical algorithm, which allows direct retrieval of wave
59 parameters from co-polarization SAR without calculating the modulation transfer
60 function (MTF) of each SAR mapping modulation.

61 The first category includes the Max-Planck Institute Algorithm (MPI)
62 (Hasselmann and Hasselmann 1991), the semi parametric retrieval algorithm (SPRA)
63 (Mastenbroek and Valk 2000), the parameterized first-guess spectrum method (PFSM)
64 (Sun and Guan 2006;) and the partition rescaling and shift algorithm (PARSA)
65 (Schulz-Stellenfleth et al. 2005; Li et al. 2010), which are independent of radar

66 frequency and polarization. These algorithms take a ‘first-guess’ wave spectrum in the
67 inversion schemes, because the velocity bunching is a non-linear modulation causing
68 signal loss in the azimuth direction. The MPI and PARSA algorithms use the
69 simulations from a numeric wave model, which takes a considerable amount of time
70 for model running in the operational application. The SPRA algorithm employs a
71 wave spectrum produced by using a parameterized empirical function in the scheme,
72 indicating it can be more conveniently applied than the MPI and PARSA algorithms.
73 Subsequently, the PFSM algorithm was developed in order to overcome the
74 model-induced error in the SPRA scheme system, which is included in the swell SAR
75 spectrum. The improvement to the PFSM algorithm is that a prior SAR spectrum is
76 divided into two portions, including wind-sea and linear-mapping swell. Through
77 searching for the most suitable parameters, a best fit ‘first-guess’ spectrum is
78 produced by a parametric wave model, which is similar to SPRA, and then an MPI
79 scheme is employed for retrieving the wind-sea spectrum. The swell spectrum is
80 obtained by directly inverting the linear-mapping SAR spectrum. Finally, the wave
81 spectrum is composited of wind-sea and swell spectrum and then significant wave
82 height (SWH) is calculated by integrating the SAR-derived wave spectrum. In our
83 previous study, it was found that the PFSM algorithm worked for C-band (Lin et al.
84 2017) and X-band SAR (Shao et al. 2015) with an approximate 0.6m root mean
85 square error (RMSE) of SWH.

86 The algorithm for quad-polarization (Q-P), which is the second category
87 (Schuler et al. 2004; He et al. 2006; Zhang et al. 2010), is aimed at wave retrieval
88 from SAR images such as the Q-P data acquired by R-2 and polarimetric SAR
89 (POL SAR). These theoretical-based algorithms are exploited based on the wave slope
90 estimation from SAR images in the co-polarization and HV-polarization channels.
91 SWH is calculated by using the SAR-derived wave slope spectrum. Because GF-3
92 SAR wave mode data is available in quad-polarization, SWH can be measured by
93 using the Q-P algorithm.

94 The empirical model is commonly used for marine applications of
95 co-polarization SAR, and is classified as the third category. The CWAVE family was
96 originally exploited by SAR oceanographers at the German Aerospace Center (DLR),
97 e.g., CWAVE_ERS (Schulz-Stellenfleth et al. 2007) for ERS-1/2 SAR and
98 CWAVE_ENV (Li et al. 2011) for ENVISAT-ASAR, and can be applied for wave
99 retrieval from SAR wave mode data at C-band without calculating the complex MTF

100 of each SAR mapping modulation. The coefficients of the CWAVE model need to be
101 refitted for a different SAR, such as the CWAVE_S1 for the European S-1 SAR
102 (Stopa and Mouche, 2017). In addition, several recent studies have developed
103 algorithms to retrieve SWH through the cutoff wavelength at C-band for R-2 (Ren et
104 al. 2015), S-1 SAR (Shao et al. 2016; Grieco et al. 2016; Stopa and Mouche, 2017). In
105 our recent study, an empirical algorithm is exploited for GF-3 SAR in co-polarization,
106 named CSAR_WAVE2 (Sheng et al. 2018). CSAR_WAVE2 employs the basic
107 formulation of the CWAVE model, in which the coefficients are tuned through 1523
108 GF-3 SAR QPS-I/II mode images with collocated European Centre for
109 Medium-Range Weather Forecasts (ECMWF) reanalysis SWH data at 0.125° grids.

110 GF-3 SAR provides available data in wave mode for oceanic wave monitoring if
111 request, similar to S-1 SAR, which has a about spatial coverage of around $5\text{km}\times 5\text{km}$
112 with a pixel size of 5m for azimuth direction and 4~6m for range direction. GF-3 SAR
113 wave mode operates in quad-polarization with alternate incidence angle ranges from
114 20° to 50° , leading to adaptability of ocean observation, although small spatial
115 coverage brings the limitation in the perspective of an operational ocean waves
116 retrieval to some extent. In particular, the product derived from the SAR wave mode
117 data is dedicated to oceanography research, particularly for global wave analysis (Li
118 2016). Therefore, for operational application, it is essential to establish the accuracy
119 of the wave retrieval data for GF-3 SAR wave mode.

120 In this study, SWH is retrieved from quad-polarization GF-3 SAR wave mode
121 data by using three algorithms, including PFSM, CSAR_WAVE2 and Q-P. Then
122 assessment is presented as retrieval results are compared with the ECMWF reanalysis
123 field at 0.125° grids. Our work shows the comparison of wave monitoring from the
124 Chinese quad-polarization GF-3 SAR wave mode data with the European Centre for
125 Medium-Range Weather Forecasts (ECMWF) reanalysis data and further recommend
126 the algorithm for the operational wave retrieval. Moreover, the accuracy of retrieval
127 SWH under various winds and sea states conditions is also studied in order to figure
128 out the limitation and future improvement of wave retrieval algorithm for GF-3 SAR
129 wave mode.

130 The remaining part of this paper is organized as follows: the datasets are briefly
131 described in Section 2. Section 3 introduces the methodology of the theoretical-based
132 and empirical wave retrieval algorithms used in this study. Then the validation of

133 retrieval results is presented in Section 4. Section 5 shows the discussion and we give
134 the summary in Section 6.

135 **2. Brief description of data**

136 The type of GF-3 SAR wave mode data is default processed as a Level-1A (L-1A)
137 production, and was collected during the period August 2016 to January 2018. We
138 take the following equation for calibrating the quad-polarization GF-3 SAR wave
139 mode data.

$$140 \quad \sigma_0 = DN^2 \times \left(\frac{M}{32767} \right)^2 - N \quad [\text{dB}] \quad (1)$$

141 where σ_0 is the normalized radar cross (NRCS) united in dB, DN is the
142 SAR-measured image intensity, M and N are the calibration constants stored in the
143 annotated file.

144 To investigate the performance of the wave algorithms for GF-3 SAR wave
145 mode, we also compared SAR-derived SWH with a $0.125 \times 0.125^\circ$ grid from the
146 ECMWF reanalysis SWH data in this study. The ECMWF provides global reanalysis
147 atmospheric and marine data for investigators world-wide, at a fine spatial resolution
148 (up to a 0.125° grid) and at an interval of 6-hours per day. To date, ECMWF
149 reanalysis data has proved a valuable source for developing and validating algorithms
150 for SAR (Hersbach et al. 2007; Hersbach et al. 2010; Li et al. 2011; Shao et al. 2017).

151 Other marine phenomena may exist in the images, e.g., ice, upwelling and eddy,
152 causing inhomogeneous patterns in the SAR scene. Therefore, homogeneous GF-3
153 SAR images acquired in wave mode were chosen in about 50% of the total cases,
154 where the ratios of image variance and squared image mean values were smaller than
155 1.05 (Li et al. 2011). As examples, a homogeneous case taken at 06:54 UTC on 10
156 April 2017 and an inhomogeneous case at 02:36 UTC on 6 February 2017 are shown
157 in Figures 1 and 2, respectively.

158 [Figure 1]

159 [Figure 2]

160 The geographical locations of all collected images are shown in Figure 3, in
161 which the incidence angle for each image is indicated by the colour used, and Figure 4
162 shows the histogram of the wind speed, incidence angle, and SWH in the data

163 collection. The available GF-3 SAR wave mode data for this study is presented in
164 Table 1, in which 10514 GF-3 SAR imageries are used in order to evaluate the
165 accuracy of SAR-derived SWH by using the three existing wave retrieval algorithms.
166 Noted that the spatial coverage of dataset collected in the two years mission is
167 limitedly, because GF-3 SAR wave mode only operates in request. Moreover, most
168 imageries were taken at middle to high incidence angle, e.g., only 497 and 87
169 imageries at the incidence angle ranged from 20° to 25° and from 25° to 30° in the
170 available dataset respectively, because we did the major quality control at such
171 condition, which is common for other GF-3 SAR imaging modes in the duration of
172 on-orbit calibration. In fact, the cooperation with NSOAS is in progress, for which
173 GF-3 SAR wave mode covers the global sea within one month, and a larger dataset is
174 anticipated.

175 [Table 1]

176 [Figure 3]

177 [Figure 4]

178 **3. Methodology of wave retrieval algorithm**

179 In this section, the principles of the three existing wave retrieval algorithms for
180 co-polarization and quad-polarization, of PFSM, CSAR_WAVE2, and Q-P, are
181 introduced.

182 **3.1 The PFSM algorithm**

183 SAR-derived wind speed U_{10} has first to be obtained as the PFSM algorithm is
184 applied for retrieving waves from SAR images. The Geophysical model function
185 (GMF) C-SARMOD (Mouche and Chapron 2015) is used here, and has the general
186 formulation:

$$187 \quad \sigma_0 = B_0 \times (1 + B_1 \times \cos\theta + B_2 \times \cos 2\theta) \quad (1)$$

188 where σ_0 is the SAR-measured NRCS usually expressed as a linear combination of
189 three terms, B_s are functions of sea surface wind speed U_{10} and radar incidence angle
190 θ , and φ is wind direction relative to range direction. Because two unknown variables
191 exist in the C-SARMOD model, wind directions from the ECMWF reanalysis field at

192 a 0.125° grid are directly employed. It should be noted that C-SARMOD is directly
193 applicable for VV- and HH-polarization without using an extra polarization ratio (PR)
194 model.

195 The PFSM algorithm scheme mainly includes two steps:

196 (1) The SAR intensity spectrum is obtained using the Fast Fourier
197 Transformation (FFT) method on the original SAR data. Eq. (2) is used to calculate
198 the separation wave number k_s . Then the SAR spectrum is divided into two portions,
199 of nonlinear-mapping wind-sea and linear-mapping swell state.

$$200 \quad k_s = \left(\frac{2.87 \times g \times V^2}{R^2 \times U_{10}^4 \times \cos^2 \varphi \times (\sin^2 \varphi \times \sin^2 \theta + \cos^2 \varphi)} \right)^{0.33} \quad (2)$$

201 in which, g is the gravity acceleration, V is the satellite flight velocity, R is the slant
202 range, U_{10} is the SAR-derived wind speed, θ is the radar incidence angle and φ is the
203 angle of wave propagation direction relative to radar look direction.

204 (2) Wind-sea and swell spectra are retrieved from the corresponding portion of a
205 SAR image spectrum. In the process of wind-sea retrieval, a ‘first-guess’ spectrum is
206 generated using the parametric Jonswap model (Hasselmann and Hasselmann 1985)
207 after searching for the most suitable parameters of wind wave spectrum, e.g.,
208 dominant wave phase velocity and wave propagation direction. Then, the wind wave
209 spectrum is retrieved by minimizing the cost function (Hasselmann and Hasselmann
210 1991). In the meantime, it is convenient to invert the linear-mapping portion of a SAR
211 image spectrum into a swell spectrum. SWH H_s is calculated through integrating the
212 composite one-dimensional wave spectrum S_k in terms of wave number k by using Eq.
213 (3).

$$214 \quad H_s = 4 \sqrt{\int S_k dk} \quad (3)$$

215 A standard deviation (STD) of 0.67m was found when comparing retrieval
216 results from 50 S-1 SAR images in VV-polarization with ECMWF reanalysis grids
217 wave data around the China Seas (Lin et al. 2017).

218

219 3.2 CSAR_WAVE2

220 Theoretically, sea state is related to azimuthal cutoff wavelength (Hasselmann
221 and Hasselmann 1991; Grieco et al. 2016; Stopa et al. 2016). Therefore, we proposed
222 a semi-empirical algorithm for SWH retrieval, denoted as CSAR_WAVE, which was

223 tuned through VV-polarization S-1 SAR images and collocated measurements from
 224 NDBC buoys of NOAA (Shao et al. 2016). In our recent study, the RMSE of SWH
 225 was found to be 0.58m using CSAR_WAVE when comparing the retrieved SWH
 226 from a few GF-3 SAR images in co-polarization with NDBC buoy measurements of
 227 NOAA (Shao et al. 2017).

228 In order to improve the accuracy of wave retrieval for GF-3 SAR, non-linear
 229 higher-order corrections on sea state are implemented in a new empirical algorithm,
 230 denoted as CSAR_WAVE2. CSAR_WAVE2 takes the basic formulation of the
 231 CWAVE family model, which assumes that sea state SWH can be connected by a set
 232 of imaging parameters with a coefficient vector (Schulz-Stellenfleth et al. 2007; Li et
 233 al. 2011; Stopa and Mouche, 2017). Schulz-Stellenfleth et al. (2007) found the
 234 RMSE of SWH to be 0.44m when using CWAVE with the second order model
 235 terms and this gives a better performance of 0.58m RMSE of the SWH when using
 236 the quadratic function for ERS-2 SAR wave mode.

237 The function of CSAR_WAVE2 is expressed as,

$$238 H_s = a_0 + \sum_{i=1}^n a_i \times s_i + \sum_{i,j=1}^n a_{i,j} \times s_i \times s_j \quad (4)$$

239 in which s_i are the imaging parameters and vector $a_{i,j}$ ($i \leq j \leq n$) are the tuned
 240 coefficients. In practice, imaging parameters s_i in the CSAR_WAVE2 model include
 241 a vector ($U_{10}, \sigma_0, cvar, \lambda_c/\beta, \sin\theta, \cos2\varphi, \lambda_{SAR}$). U_{10} is the inverted wind speed, σ_0 is
 242 the SAR-measured NRCS, λ_c is the azimuthal cutoff wavelength estimated by fitting
 243 a one-dimensional SAR spectrum with a Gaussian fit function, θ is radar incidence
 244 angle φ peak wave direction relative to range direction ranged from 0° to 90° , β is
 245 the satellite range-to-velocity parameter, λ_{SAR} is the SAR length at peaks of the SAR
 246 spectrum and $cvar$ is the normalized SAR image stated as,

$$247 cvar = \text{var}\left(\frac{I - \bar{I}}{\bar{I}}\right) \quad (5)$$

248 where, I is the pixel intensity of the SAR image and \bar{I} is the mean of intensity.

249 It can be seen from our recent study (Sheng et al. 2018) that the RMSE of the
 250 SWH is about 0.52m for co-polarization GF-3 SAR imaging mode acquired in
 251 QPS-I/II when retrieval results are compared with the measurements from altimeter
 252 Jason-2. It was also found that CSAR_WAVE2 has a better performance of wave
 253 retrieval for GF-3 SAR than the analysis results achieved when using the other
 254 empirical algorithms proposed in Wang et al. (2012), Ren et al. (2015) and Grieco et
 255 al. (2016).

256

257 3.3 Algorithm Q-P

258 GF-3 wave mode is an available C-band SAR acquired in quad-polarization for
259 wave monitoring over global seas. In recent years, efforts have been made to retrieve
260 quantitative waves from quad-polarization SAR images (Schuler et al. 2004; He et al.
261 2006; Zhang et al. 2010).

262 The main principle of algorithm Q-P is that ocean waves sloping in the azimuth
263 and range directions can be directly obtained using SAR data in the different
264 polarization channels, e.g., HH-, VV- and HV-polarization. On the other hand, sea
265 state is related to ocean wave slope. Taken together, SWH can be conveniently
266 retrieved from a SAR-derived wave slope spectrum. The advantage of the Q-P
267 algorithm is that wave parameters can be directly extracted from quad-polarization
268 SAR images without estimating the complex hydrodynamic MTFs, similar to the
269 empirical algorithms.

270 The Q-P algorithm procedure is illustrated as follows.

271 (1) Based on SAR images in the HH-, VV- and HV-polarization channel, the
272 linearly polarized images σ_p are calculated using the following equation, in which the
273 polarization orientation angle ψ is set as 45° .

$$274 \quad \sigma_p = \frac{1}{4}(\sigma_{HH} + \sigma_{VV}) \cdot [1 + \cos^2(2\psi)] + \frac{1}{2}(\sigma_{HH} - \sigma_{VV}) \cdot \left[\sigma_{HV} + \frac{1}{2} \times \Re[\sigma_{HHVV}] \times \sin^2(2\psi) \right] \quad (6)$$

275 in which σ_{VV} , σ_{HH} , and σ_{HV} represent the NRCS in the corresponding channel, σ_{HHVV}
276 is correlated between HH- and VV- polarization and $\Re[]$ represents the real parts of
277 the indicated quantities.

278 (2) The wave slope spectrum ζ in range $\partial\zeta/\partial x$ and azimuth direction $\partial\zeta/\partial y$ is
279 estimated using Eqs. (7a) and (7b),

$$280 \quad \frac{\Delta\sigma_{VV}}{\sigma_{VV}} - \frac{\Delta\sigma_{HH}}{\sigma_{HH}} = -\frac{8 \times \tan\theta}{1 + \tan^2\theta} \times \frac{\partial\zeta}{\partial x} \quad (7a)$$

$$281 \quad \frac{\Delta\sigma_p}{\sigma_p} - \frac{\Delta\sigma_{VV}}{\sigma_{VV}} = A \times \frac{\partial\zeta}{\partial x} + B \times \frac{\partial\zeta}{\partial y} \quad (7b)$$

282 in which the coefficients A and B are referred to in Eq. 80 proposed in He et al.
283 (2006).

284 (3) The root mean square slopes S_{rms} through the $\partial\zeta/\partial x$ and $\partial\zeta/\partial y$, together with
285 the dominant wave propagation direction ϕ are calculated using the following
286 equation,

287
$$S_{rms} = \sqrt{\left(\left\langle \frac{\partial \xi}{\partial x} \times \sin \phi \right\rangle\right)^2 + \left(\left\langle \frac{\partial \xi}{\partial y} \times \cos \phi \right\rangle\right)^2} \quad (8)$$

288 (4) SWH H_s is calculated with Eq. (9),

289
$$H_s = 2\sqrt{2} \times S_{rms} \quad (9)$$

290 **4. Validations**

291 In this section, we first present a comparison of the SAR-derived wind speed with
 292 ECMWF reanalysis data at 0.125° grids, as wind speed is directly related to sea state
 293 and is used in the wave retrieval algorithms. Then the retrieved SWHs are validated
 294 against the ECMWF reanalysis data by using the existing algorithms PFSM,
 295 CSAR_WAVE2 and Q-P.

296 4.1 Comparison of SAR-derived wind speed

297 The non-Bragg contribution on radar backscattering at VV-polarization is
 298 smaller than that at HH-polarization (Phillips et al. 2001; Kudryavtsev et al. 2003),
 299 which indicates that the wind and wave retrieval algorithms perform better at
 300 VV-polarization. Therefore, a comparison of retrieved wind speeds from GF-3 SAR
 301 images acquired in wave mode at VV-polarization is presented here.

302 As shown in Eq. (1), there are two unknown variables in the C-SARMOD. In
 303 this study, wind directions are obtained through ECMWF reanalysis data using the
 304 bilinear interpolation at temporal and spatial scales. Then wind speed can be retrieved
 305 from GF-3 SAR images acquired in wave mode. Figure 5 shows SAR-derived wind
 306 speeds using C-SARMOD versus wind speeds from ECMWF reanalysis data for
 307 0.25m/s of wind speed bins between 0 and 15m/s. The RMSE of wind speed was
 308 found to be about 1.8m/s, which is close to the 1.6m/s and 1.4m/s RMSEs of wind
 309 speed against a few NDBC buoys of NOAA when C-SARMOD was applied for
 310 VV-polarization S-1 SAR (Lin et al. 2017) and GF-3 SAR (Shao et al. 2017) acquired
 311 in imaging mode. The worse performance here was probably caused by the use of
 312 different sources for validation. However, this still illustrates that SAR-derived wind
 313 speeds are reliable in the process of wave retrieval. It should be noted that the
 314 retrieved winds are smaller than 20m/s and do not have the backscattering signal

315 problem encountered in the application of traditional GMF algorithms for wind
316 retrieval at higher winds (Hwang et al. 2015).

317 [Figure 5]

318 4.2 Comparison of SAR-derived SWH

319 We first present the retrieval results of a sub-scene extracted from the images
320 taken on 10 April 2017 at 06:54 UTC when using the existing three algorithms. In this
321 case, the SWH from the ECMWF reanalysis data is 1.85m.

322 A quick-look image of the sub-scene covering the ECMWF locations at the
323 0.125° grid points is shown in Figure 6a as an example of retrieval results and the
324 corresponding two-dimensional SAR spectrum is shown in Figure 6b. The
325 SAR-derived SWH is 1.37m when using the PFSM algorithm through the retrieved
326 one-dimensional wave spectrum exhibited in Figure 6c. The azimuthal cutoff
327 wavelength λ_c is usually calculated by fitting a SAR spectrum with a Gaussian fit
328 function $\exp\{\pi(k_x/k_c)\}$, in which k_x is the azimuthal wavenumber and $k_c=2\pi/\lambda_c$ is the
329 azimuthal cutoff wavenumber. Figure 6d shows the Gaussian fitted result of a
330 sub-scene and the retrieved SWH is 2.37m using the CSAR_WAVE2 empirical
331 algorithm. The SAR slope spectrum of the case is shown in Figure 7a and
332 SAR-derived SWH is 1.45m using the Q-P algorithm through the retrieved
333 one-dimensional wave slope spectrum, as exhibited in Figure 7b.

334 [Figure 6]

335 [Figure 7]

336 The collected sub-scenes from GF-3 SAR images were considered in order to
337 evaluate the accuracy of SAR-derived SWH. The retrieved results were compared
338 with ECMWF reanalysis data. In general, Figure 8 shows a 0.57m RMSE of SWH
339 with a 0.22 scatter index (SI) using CSAR_WAVE2, which is less than a 0.63m
340 RMSE with a 0.24 SI and a 0.71m RMSE with a 0.26 SI achieved using the PFSM
341 algorithm and the Q-P algorithm respectively. It is not surprising that CSAR_WAVE
342 has the best performance at low to moderate sea state, because CSAR_WAVE2 is
343 directly tuned through GF-3 SAR data and the non-linearity among different imaging
344 parameters has been included in the tune process of algorithm. A further comparison

345 for a 1 m bin of SWH is also presented in Figure 8. It is found that RMSE of SWH is
346 0.47 m using PFSM algorithm and 0.43 m using CSAR_WAVE2 at SWH between
347 2m and 3m, which are less than that at other SWH ranges, however, Q-P algorithm
348 has a worse performance (a 0.85 m RMSE) at such condition.

349 [Figure 8]

350 **5. Discussions**

351 We also analyze the applicability of the empirical algorithm CSAR_WAVE2 in
352 various conditions. The bias (SAR-derived SWH minus SWH from ECMWF) versus
353 the incidence angle and wind speed from ECMWF are shown in Figures 9a and 9b,
354 respectively. A bin size of 2° for incidence angle and 1m/s for wind speed is used to
355 group data pairs and the error bars represent the standard deviation of each bin. It is
356 difficult to make state about the relation between the variation of bias and incidence
357 angle. Interestingly, the variation of bias remains about 0.2m at wind speeds greater
358 than 5m, indicating wind speed has little impact on bias with increasing wind speed.

359 [Figure 9]

360 The variation of bias as a function of SWH along with the ECMWF SWH for a
361 bin size of 0.5m is presented in Figure 9c. It is roughly shown that the retrieved SWH
362 over-estimates at SWH smaller than 2.5m and retrieved SWH has an underestimation
363 at SWH greater than 2.5m. Nevertheless, it is clear to observe that the retrieval error
364 grows with decreasing SWH at low state (SWH probably smaller than 2m). It is well
365 known that cutoff wavelength in azimuth direction represents the velocity bunching
366 mechanism, which is proportional to SWH (Hasselmann and Hasselmann 1991).
367 Therefore, Bragg waves at sea surface with wavelength smaller than the cutoff
368 wavelength in azimuth direction quantitatively decrease under low sea state condition,
369 due to cutoff wavelength in azimuth direction is relatively small at such condition. In
370 other words, SAR backscattering signal is weak at low sea state. This is the probable
371 explanation for the decreasing accuracy with decreasing SWH smaller than 2m,
372 causing the limitation of CSAR_WAVE2. This issue needs to be resolved in the
373 improvement of the wave retrieval algorithm for GF-3 SAR acquired in wave mode.

374 **6. Summary**

375 GF-3 SAR, operating in wave mode with alternate incidence angle, has the capability
376 to monitor waves in global seas. At present, three algorithms, PFSM, CSAR_WAVE2
377 and Q-P, are considerably applied for wave retrieval from SAR images. As to release
378 an operational product for global monitoring, it is necessary to select an optimal wave
379 retrieval algorithm through evaluating the accuracy of SWH retrieval. Our work
380 clarifies this issue through the comparison between the GF-3 image acquired in wave
381 mode with the ECMWF model data, although taking advantage of limit dataset
382 collected in the last two years mission.

383 A total of 10541 homogeneous cases from the collected images were selected,
384 and these were matched up with ECMWF reanalysis data at 0.125° grids. GMF
385 C-SARMOD was employed to retrieve winds for GF-3 SAR at VV-polarization,
386 which was assumed to be prior information in the process of wave retrieval. The
387 comparison shows a 1.8m/s RMSE of wind speed against the wind speed from the
388 ECMWF reanalysis data, which is close to the accuracy of its application for S-1
389 SAR.

390 The 10514 images were processed using the three algorithms. The retrieved
391 results were compared with SWH from ECMWF reanalysis wave data, and showed
392 the RMSE of SWH to be 0.57m, 0.63m and 0.71m when using the PFSM,
393 CSAR_WAVE2 and Q-P algorithms. However, we found that the SAR-derived SWH
394 had a trend of saturation at SWH ranging up to 1.4m when using the Q-P algorithm,
395 implying that retrieved SWH has an ambiguity under such conditions.

396 In summary, although our work shows that the CSAR_WAVE2 is recommended
397 for use with GF-3 SAR data acquired in wave mode to date, we realize an
398 improvement of the wave retrieval algorithm is still anticipated to ensure a better
399 applicability for GF-3 SAR wave mode, especially the Chinese operational SAR
400 satellite GF-3B and 3C plans to be launched at the end of 2019.

401 **Acknowledgements**

402 GF-3 SAR images are collected through an authorized account issued by
403 NSOAS via <http://dds.nsoas.org.cn>. We also kindly appreciate ECMWF provides
404 wind and wave data, which were openly downloaded via <http://www.ecmwf.int>. The
405 research is partly supported by the National Key Research and Development Program
406 of China under contract No. 2017YFA0604901, National Natural Science Foundation
407 of China under contract No. 41806005, Public Welfare Technical Applied Research

408 Project of Zhejiang Province of China under contract No. LGF19D060003 and
409 New-Shoot Talented Man Plan Project of Zhejiang Province under contract No.
410 2018R411065.

411 **6. References**

412 Alpers, W., Ross, D. B. and Rufenach, C. L. 1981. "On the detectability of ocean
413 surface waves by real and synthetic radar." *Journal of Geophysical Research*,
414 Vol. 86 (No. C7): pp. 6481–6498. doi: 10.1029/JC086iC07p06481.

415 Alpers, W. and Bruning, C. 1986. "On the relative importance of motion-related
416 contributions to the SAR imaging mechanism of ocean surface waves." *IEEE*
417 *Transactions on Geosciences and Remote Sensing*, Vol. GE-24 (No. 6): pp.
418 873–885. doi: 10.1109/TGRS.1986.289702.

419 Chapron, B., Johnsen, H. and Garello, R. 2001. "Wave and wind retrieval from SAR
420 images of the ocean." *Annales Des Télécommunications*, Vol. 56 (No. 11): pp.
421 682–699. doi: 10.1007/BF02995562.

422 Feindt, F., Schroter, J. and Alpers, W. 1986. "Measurement of the ocean wave-radar
423 modulation transfer function at 35GHz from a sea-based platform in the North
424 Sea." *Journal of Geophysical Research*, Vol. 91 (No. C8): pp. 9701–9708. doi:
425 10.1029/JC091iC08p09701.

426 Grieco, G., Lin, W., Migliaccio, M., Nirchio, F. and Portabella, M. 2016.
427 "Dependency of the Sentinel-1 azimuth wavelength cut-off on significant wave
428 height and wind speed." *International Journal of Remote Sensing*, Vol. 37 (No.
429 21): pp. 9701–9708. pp. 5086–5104. doi: 10.1080/01431161.2016.1226525.

430 Hasselmann S. and Hasselmann K. 1985. "Computations and parametrizations of the
431 nonlinear energy transfer in a gravity-wave spectrum. I: a new method for
432 efficient computations of the exact nonlinear transfer integral." *Journal of*
433 *Physical Oceanography*, Vol. 15 (No. 1985): pp 1369–1377. doi:
434 10.1175/1520-0485(1985)015<1369:CAPOTN>2.0.CO;2.

435 Hasselmann, K. and Hasselmann, S. 1991. "On the nonlinear mapping of an ocean
436 wave spectrum into a synthetic aperture radar image spectrum." *Journal of*
437 *Geophysical Research*, Vol. 96 (No. C6): pp.10713–10729. doi:
438 10.1029/91JC00302.

- 439 He, Y. J., Shen, H. and Perrie, W. 2006. "Remote sensing of ocean waves by
440 polarimetric SAR." *Journal of Atmospheric and Oceanic Technology*, Vol. 23
441 (No. 12): pp.1768–1773. doi: 10.1175/JTECH1948.1.
- 442 Hersbach, H., Stoffelen, A. and Haan, S. D. 2007. "An improved C-band
443 scatterometer ocean geophysical model function: CMOD5." *Journal of*
444 *Geophysical Research*, Vol. 112 (No. C3): pp. C03006. doi:
445 10.1029/2006JC003743.
- 446 Hersbach, H. 2010. "Comparison of C-Band scatterometer CMOD5.N equivalent
447 neutral winds with ECMWF." *Journal of Atmospheric and Oceanic Technology*,
448 Vol. 27 (No. 4): pp. 721–736. doi: 10.1175/2009JTECHO698.1.
- 449 Hwang, P. A. and Fois, F. 2015. "Surface roughness and breaking wave properties
450 retrieved from polarimetric microwave radar backscattering." *Journal of*
451 *Geophysical Research*, Vol. 120 (No. 5): pp. 3640–3657. doi:
452 10.1002/2015JC010782.
- 453 Lyzenga, D. R. 1986. "Numerical simulation of synthetic aperture radar image spectra
454 for ocean waves." *IEEE Transactions on Geosciences and Remote Sensing*, Vol.
455 GE-24 (No. 6): pp. 863–872. doi: 10.1109/TGRS.1986.289701.
- 456 Li, X. M., Konig, T., Schulz-Stellenfleth, J. and Lehner, S. 2010. "Validation and
457 intercomparison of ocean wave spectra inversion schemes using ASAR wave
458 mode data." *International Journal of Remote Sensing*, Vol. 31 (No. 17): pp.
459 4969–4993. doi: 10.1080/01431161.2010.485222.
- 460 Díaz-Méndez, G. M., Lehner, S., Ocampo-Torres, F. J., Li, X. M. and Brusch, S. 2010.
461 "Wind and wave observations off the south Pacific Coast of Mexico using
462 TerraSAR-X imagery." *International Journal of Remote Sensing*, Vol. 31 (No.
463 17): pp. 4933–4955. doi: 10.1080/01431161.2010.485217.
- 464 Li, X. M., Lehner, S. and Bruns, T. 2011. "Ocean wave integral parameter
465 measurements using Envisat ASAR wave mode data." *IEEE Transactions on*
466 *Geosciences and Remote Sensing*, Vol. 49 (No. 1): pp. 155–174. doi:
467 10.1109/TGRS.2010.2052364.
- 468 Li, X. M. 2016. "A new insight from space into swell propagation and crossing in the
469 global oceans." *Geophysical Research Letters*, Vol. 43 (No. 10): pp. 5202–5209.
470 doi: 10.1002/2016GL068702.
- 471 Lin, B., Shao, W. Z., Li, X. F., Li, H., Du, X. Q., Ji, Q. Y. and Cai L. N. 2017.
472 "Development and validation of an ocean wave retrieval algorithm for

473 VV-polarization Sentinel-1 SAR data.” *Acta Oceanologica Sinica*, Vol. 36 (No.
474 7): pp. 95–101. doi: 10.1007/s13131-017-1089-9.

475 Mastenbroek, C. and Valk, C. F. de. 2000. “A semi-parametric algorithm to retrieve
476 ocean wave spectra from synthetic aperture radar.” *Journal of Geophysical
477 Research*, Vol. 105 (No. C2): pp. 3497–3516. doi: 10.1029/1999JC900282.

478 Mouche, A.A. and Chapron, B., 2015. “Global C-Band Envisat, RADARSAT-2 and
479 Sentinel-1 SAR measurements in co-polarization and cross-polarization.”
480 *Journal of Geophysical Research*, Vol. 120 (No. 11): pp. 7195–7207. doi:
481 10.1002/2015JC011149.

482 Kudryavtsev, V., Hauser, D., Caudal, G. and Chapron B. 2003. “A semiempirical
483 model of the normalized radar cross section of the sea surface, 2. Radar
484 modulation transfer function.” *Journal of Geophysical Research*, Vol. 108 (No.
485 C3): pp. FET 3-1– FET 3-16. doi: 10.1029/2001JC001004.

486 Phillips, O. M., Posner, F. L. and Hansen, J. P. 2001. “High range resolution radar
487 measurements of the speed distribution of breaking events in wind-generated
488 ocean waves: surface impulse and wave energy dissipation rates.” *Journal
489 Physical Oceanography*, Vol. 31(No. 2): 450–460. doi:
490 10.1175/1520-0485(2001)031<0450:HRRRMO>2.0.CO;2.

491 Ren, L., Yang, J. S., Zheng, G. and Wang, J. 2015. “Significant wave height
492 estimation using azimuth cutoff of C-band RADARSAT-2 single-polarization
493 SAR images.” *Acta Oceanologica Sinica*, Vol. 34 (No. 12): pp. 1–9. doi:
494 10.1007/s13131-015-0769-6.

495 Ren, L., Yang J. S., Mouche, A. A., Wang, H., Wang, J. and Zheng, G. 2017.
496 “Preliminary analysis of Chinese GF-3 SAR quad-polarization measurements to
497 extract winds in each polarization.” *Remote Sensing*, Vol. 9 (No. 12): pp: 1215.
498 doi: 10.3390/rs9121215.

499 Schuler, D. L., Lee, J. S., Kasilingam, D. and Pottier, E. 2004. “Measurement of
500 ocean surface slopes and wave spectra using polarimetric SAR image data.”
501 *Remote Sensing of Environment*, Vol. 91 (No. 2): pp: 198–211. doi:
502 10.3390/rs9121215.

503 Schulz-Stellenfleth, J., Lehner, S. and Hoja, D. 2005. “A parametric scheme for the
504 retrieval of two-dimensional ocean wave spectra from synthetic aperture radar
505 look cross spectra.” *Journal of Geophysical Research*, Vol. 101 (No. C5): pp.
506 297–314. doi: 10.1016/j.rse.2004.03.008.

507 Schulz-Stellenfleth, J., Konig, T. and Lehner, S. 2007. "An empirical approach for the
508 retrieval of integral ocean wave parameters from synthetic aperture radar data."
509 *Journal of Geophysical Research*, Vol. 42 (No. 34): pp. 10182–10190. doi:
510 10.1029/2006JC003970.

511 Shao W. Z., Li, X. F. and Sun J. 2015. "Ocean wave parameters retrieval from
512 TerraSAR-X images validated against buoy measurements and model results."
513 *Remote Sensing*, Vol. 7 (No. 10): pp. 12815. doi: 10.3390/rs71012815.

514 Shao, W. Z., Zhang, Z., Li X. F. and Li, H. 2016. "Ocean wave parameters retrieval
515 from Sentinel-1 SAR imagery." *Remote Sensing*, Vol. 8 (No. 9): pp. 707. doi:
516 10.3390/rs8090707.

517 Stopa J. E., Ardhuin, F., Chapron, B. and Collard, F. 2016. "Estimating wave orbital
518 velocity through the azimuth cutoff from space-borne satellites." *Journal of*
519 *Geophysical Research Oceans*, Vol. 120 (No. 11): pp 7616–7634. doi:
520 10.1002/2015JC011275.

521 Shao, W. Z., Shen, Y. X. and Sun, J. 2017. "Preliminary assessment of wind and
522 wave retrieval from Chinese Gaofen-3 SAR imagery." *Sensors*, Vol. 17 (No. 8):
523 pp. 1705. doi: 10.3390/s17081705.

524 Stopa, J. E. and Mouche, A. 2017. "Significant wave heights from Sentinel-1 SAR:
525 validation and applications." *Journal of Geophysical Research Oceans*, Vol. 122
526 (No. 3): pp. 1827–1848. doi: 10.1002/2016JC012364.

527 Shao, W. Z., Yuan, X. Z., Sheng, Y. X., Sun, J., Zhou, W. and Zhang, Q. J. 2018.
528 "Development of wind speed retrieval from cross-polarization Chinese Gaofen-3
529 synthetic aperture radar in typhoons." *Sensors*, Vol. 18 (No. 2): pp. 412. doi:
530 10.3390/s18020412.

531 Wang, H., Yang, J. S., Mouche, A. A., Shao, W. Z., Zhu, J. H., Ren, L. and Xie, C. H.
532 2017. "GF-3 SAR ocean wind retrieval: The first view and preliminary
533 assessment." *Remote Sensing*, Vol. 9 (No. 7): pp. 694–706. doi:
534 10.3390/rs9070694.

535 Sheng Y. X., Shao, W. Z., Zhu, S., Sun, J., Yuan, X. Z., Li, S. Q., Shi, J. and Zuo J. C.
536 2018. "Validation of significant wave height retrieval from co-polarization
537 Chinese Gaofen-3 SAR imagery by using an improved algorithm." *Acta*
538 *Oceanologica Sinica*, Vol. 37 (No. 6): pp. 1–10. doi: 10.1007/s1313.

539 Zhang, B., Perrie, W. and He, Y. J. 2010. "Validation of RADARSAT-2 fully
540 polarimetric SAR measurements of ocean surface waves." *Journal of*

541 *Geophysical Research*, Vol. 116 (No. C6): pp. 302–315. doi:
542 10.1029/2009JC005887.
543 Zhang, B., Li, X. F., Perrie, W., and He, Y. J. 2015. “Synergistic measurements of
544 ocean winds and waves from SAR.” *Journal of Geophysical Research Oceans*,
545 Vol. 120 (No. 9): pp. 6164–6184. doi: 10.1002/2015JC011052.

546

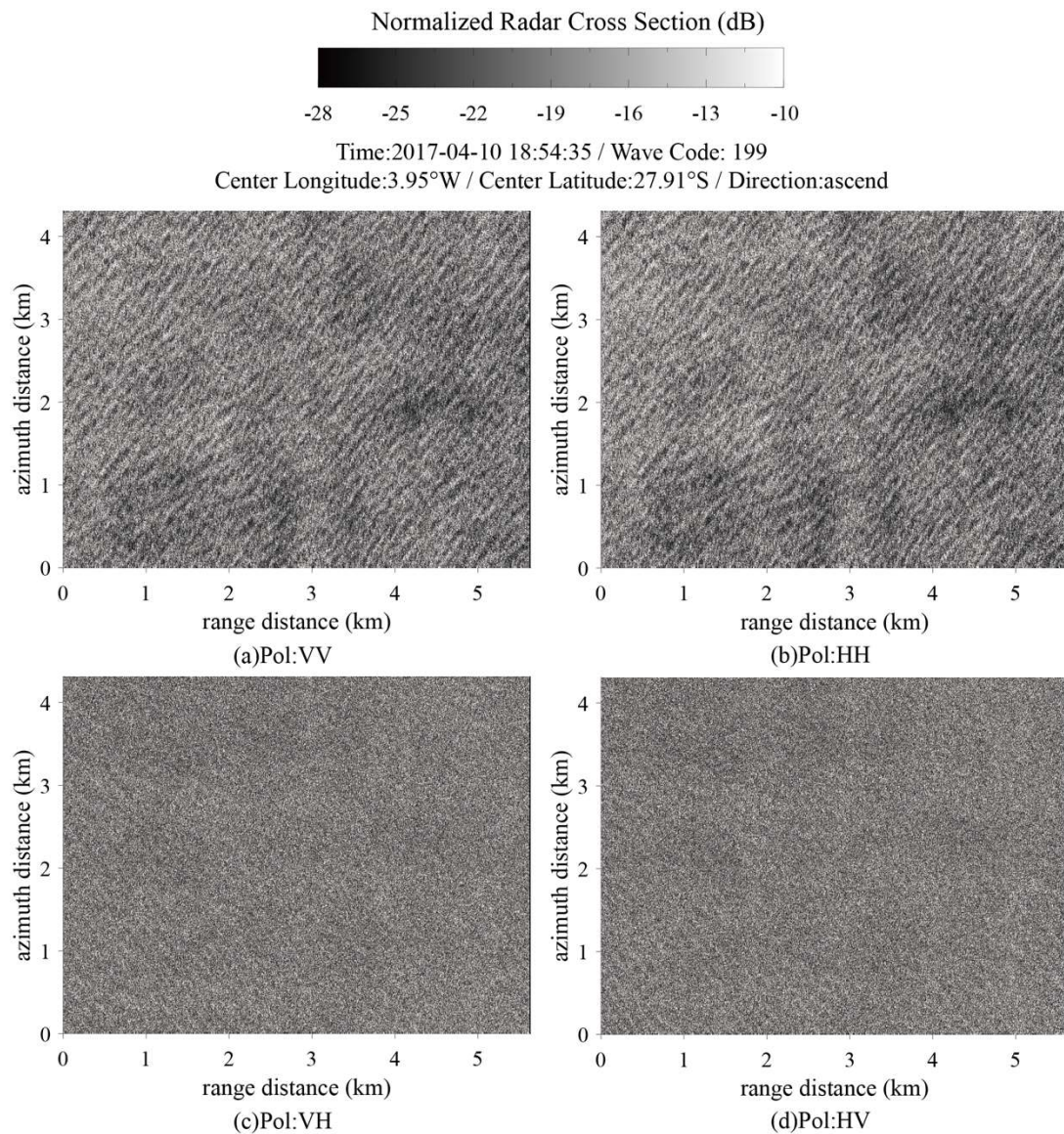
Table 1 Available Gaofen-3 (GF-3) SAR wave mode data in this study

ID	Incidence angle			Numbers of GF-3 imageries in wave mode
	Range	Mean	Standard deviation	Available numbers
WV01	20°-25°	21.93°	0.90°	497
WV02	25°-30°	28.22°	0.26°	87
WV03	30°-35°	31.30°	1.37°	1919
WV04	35°-40°	36.76°	1.20°	4605
WV05	40°-45°	42.35°	1.64°	2191
WV06	45°-50°	47.08°	1.45°	1215

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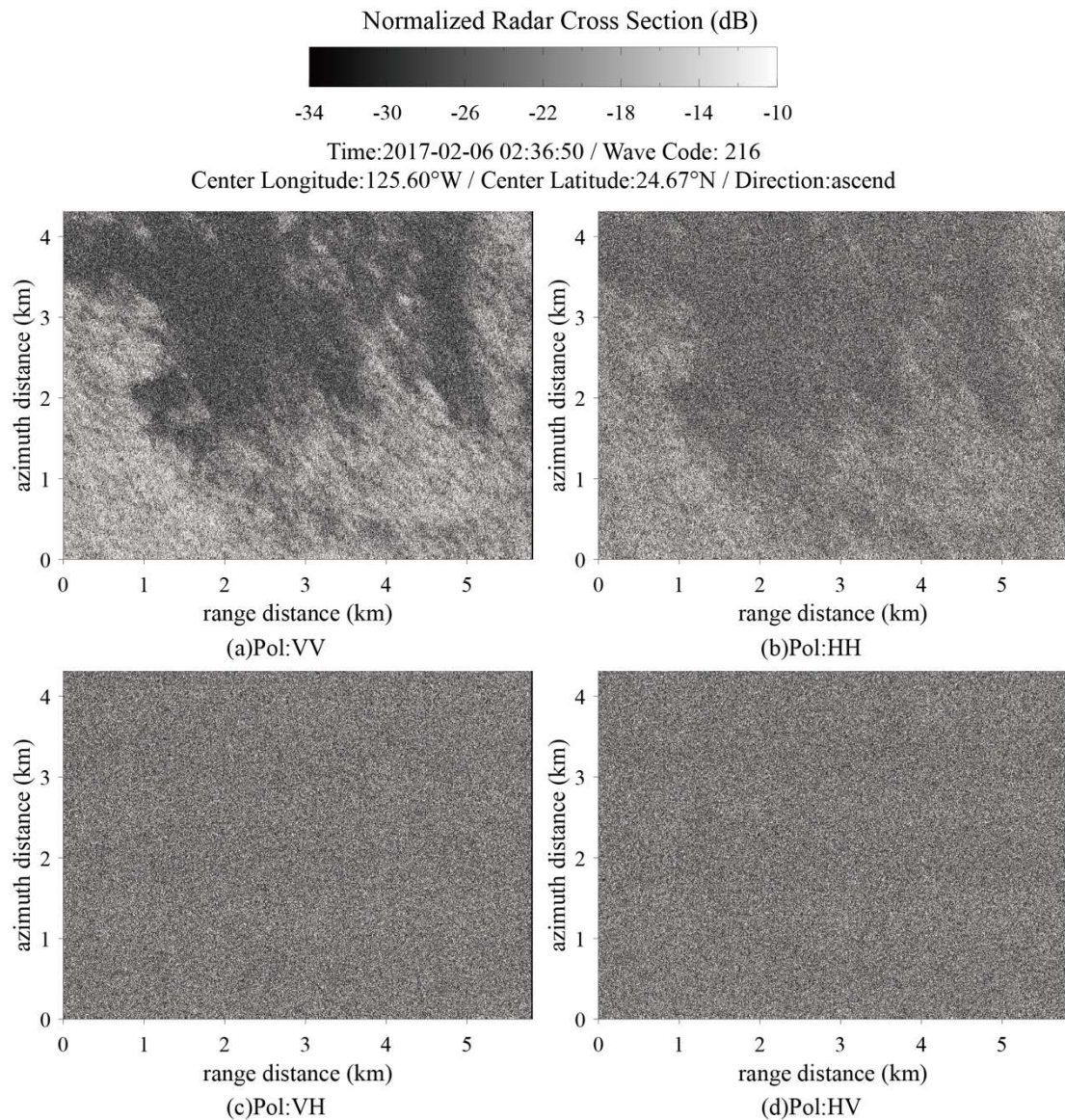
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550

551 Fig.1 An example of GF-3 SAR wave mode data with homogeneous wave streaks
552 taken at 06:46 UTC on 8 March 2017 after calibration. (a) VV-polarization. (b)
553 HH-polarization. (c) VH-polarization. (d) HV-polarization

554

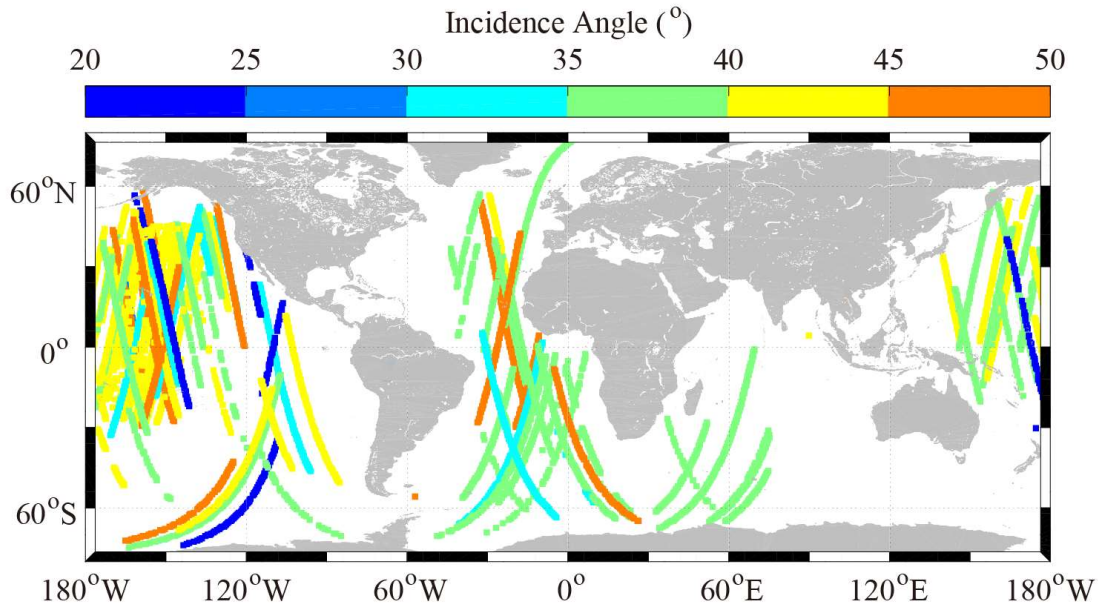


555

556 Fig.2 An example of GF-3 SAR wave mode data with inhomogeneous wave streaks
 557 taken at 02:36 UTC on 6 February 2017 after calibration. (a) VV-polarization. (b)
 558 HH-polarization. (c) VH-polarization. (d) HV-polarization

559

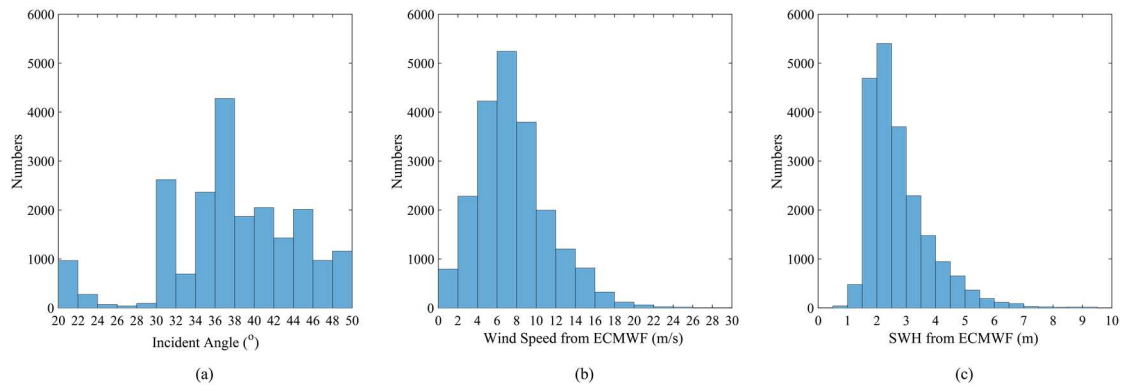
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562 Fig.3 The geographical locations of all available GF-3 SAR imageries acquired in
 563 wave mode, in which that colors show the approximate incidence angle of each
 564 imagery.

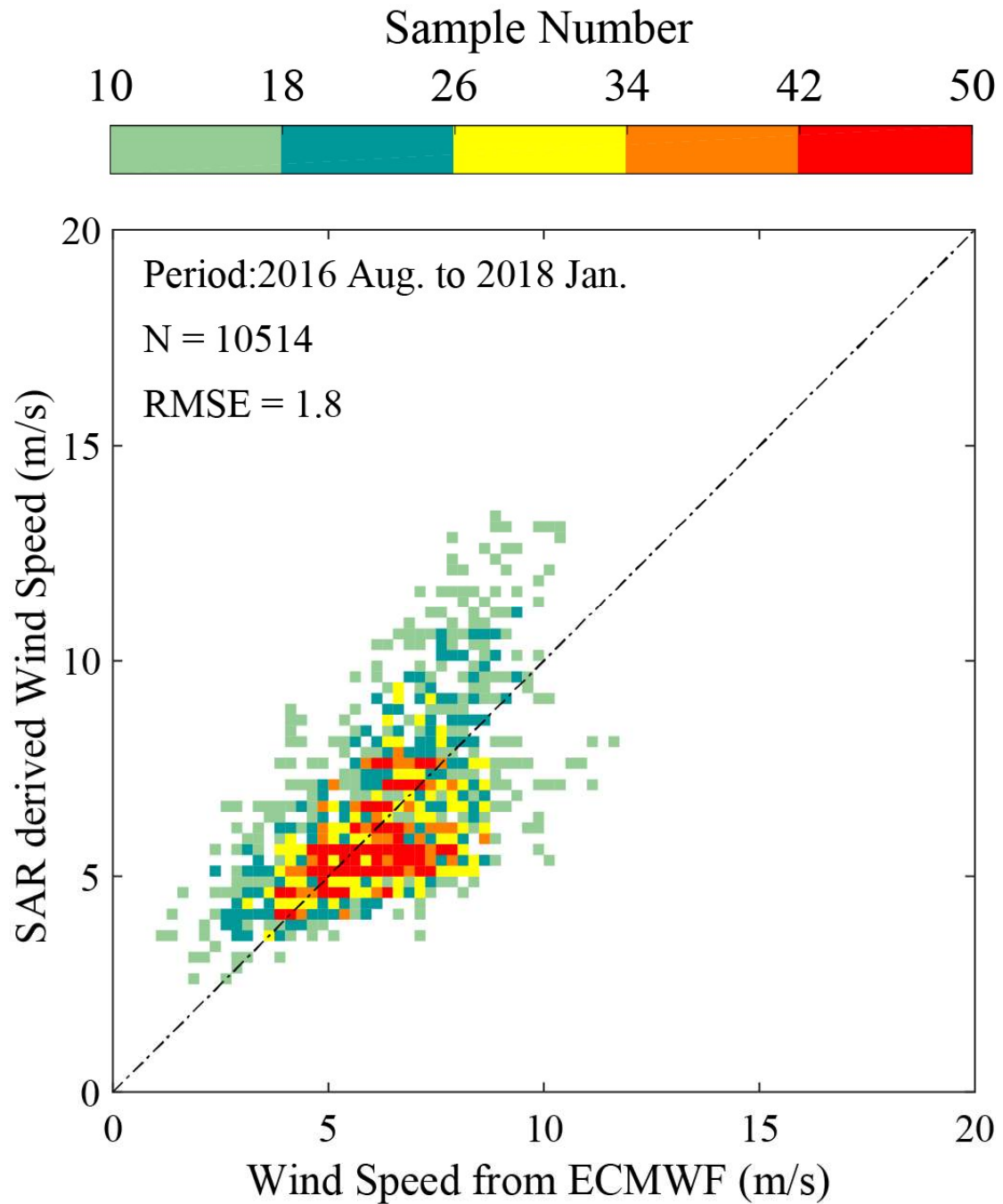
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567 Fig.4 (a) The histogram of incidence angle for the collected images. (b) The
 568 histogram of wind speed for the collected images. (c) The histogram of significant
 569 wave height for the collected images.

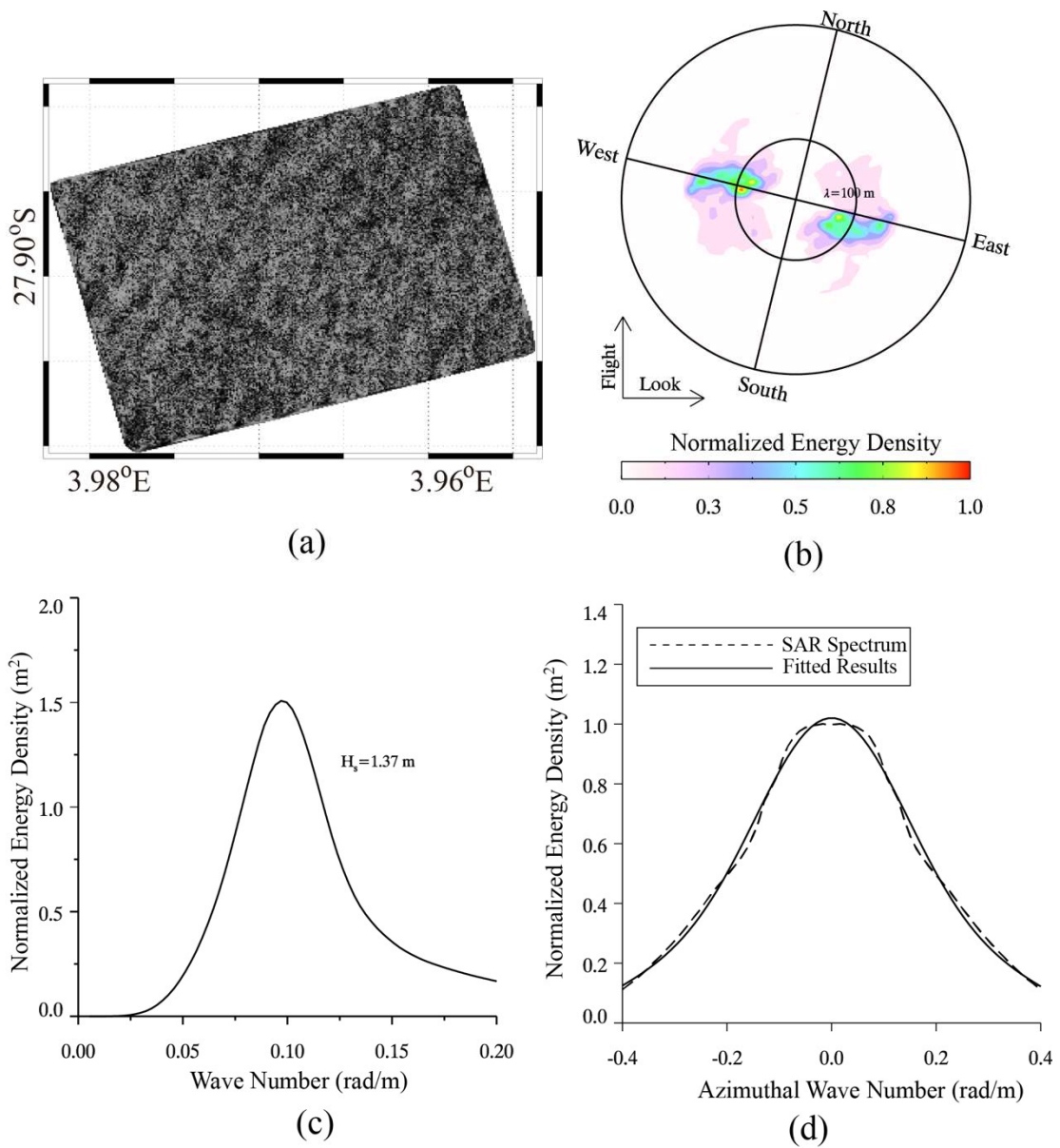
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572 Fig.5 SAR-derived wind speeds using the C-SARMOD wind retrieval algorithm
 573 versus wind speeds from ECMWF reanalysis data for 0.25m/s of wind speed bins
 574 between 0 and 15m/s.

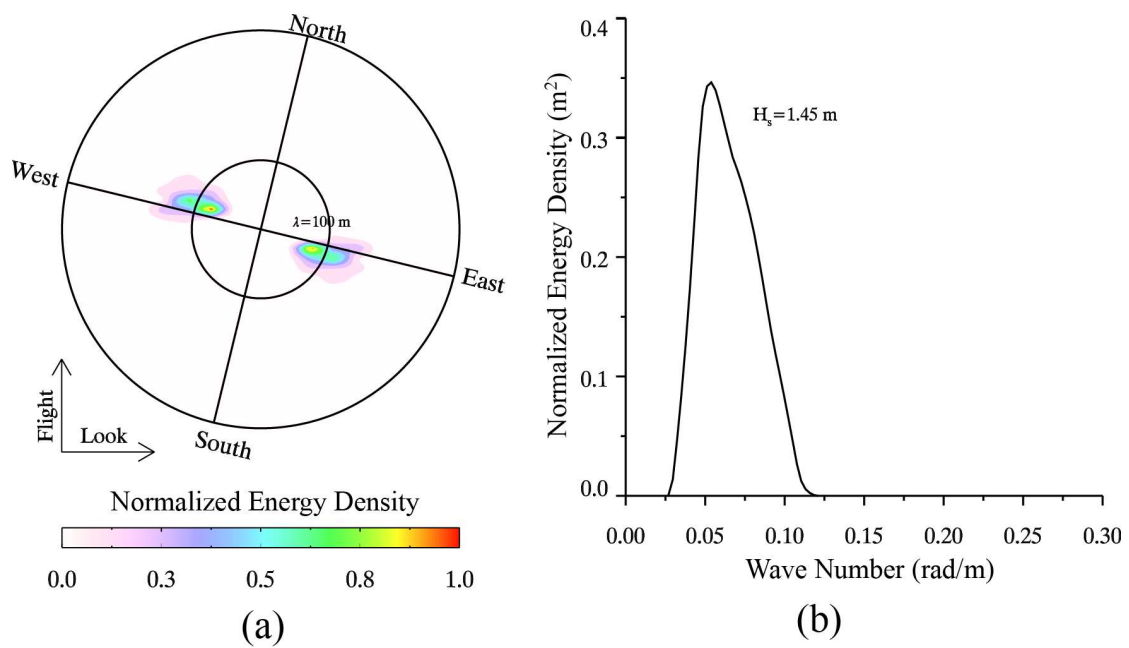
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Fig.6 (a) The sub-scene extracted from the case in VV-polarization, which was taken on 10 April 2017 at 06:54 UTC. (b) The two-dimensional SAR spectra of sub-scene in polar coordinate. (c) The SAR-derived one-dimensional wave of sub-scene. (d) The Gaussian fit result of sub-scene.

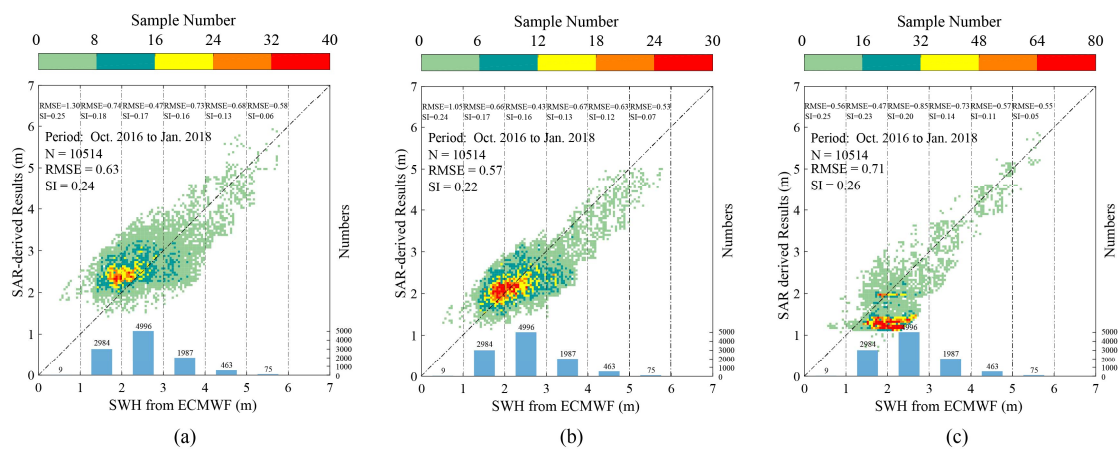
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584 Fig.7 (a) The two-dimensional SAR slope spectrum of sub-scene in polar coordinate
585 which was taken on 10 April 2017 at 06:54 UTC. (b) The SAR-derived
586 one-dimensional wave slope spectrum of sub-scene.

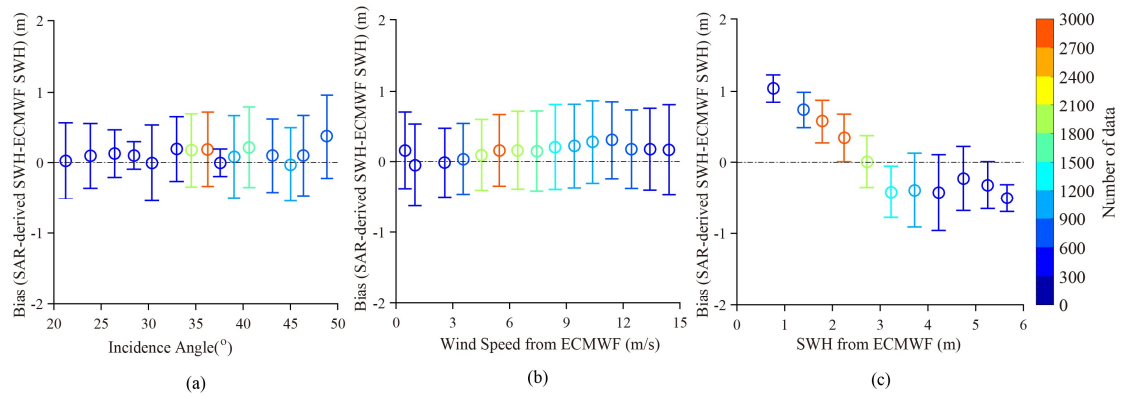
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589

590 Fig.8 SAR-derived results versus SWH from ECMWF reanalysis data for 0.05m of SWH bins
 591 between 0 and 6m when using the three existing algorithms. (a) Algorithm PFSM. (b) C Algorithm
 592 SAR_WAVE2. (c) Algorithm Q-P.

593



594

595 Fig.9 Variation of bias between SAR-derived SWH by using CSAR_WAVE2 and other parameters.

596 (a) Incidence Angle. (b) ECMWF Wind Speed. (c) ECMWF SWH.

597