

1 **Wide-spread inconsistency in estimation of lake mixed depth impacts interpretation of**  
2 **limnological processes**

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## 11 **Abstract**

12 The mixed layer, or epilimnion, is a physical concept referring to an isothermal layer at the  
13 surface of a water body. This concept is ubiquitous within limnology, is fundamental to our  
14 understanding of chemical and ecological processes, and is an important metric for water  
15 body monitoring, assessment and management. Despite its importance as a metric, many  
16 different approaches to approximating mixed depth currently exist. Using data from field  
17 campaigns in a small meso-eutrophic lake in the UK in 2016 and 2017 we tested whether  
18 different definitions of mixed depth resulted in comparable estimates and whether variables  
19 other than temperature could be assumed to be mixed within the layer. Different methods  
20 resulted in very different estimates for the mixed depth and ecologically important variables  
21 were not necessarily homogeneously spread through the epilimnion. Furthermore, calculation  
22 of simple ecologically relevant metrics based on mixed depth showed that these metrics were  
23 highly dependent on the definition of mixed depth used. The results demonstrate that an  
24 idealised concept of a well-defined fully mixed layer is not necessarily appropriate. The  
25 widespread use of multiple definitions for mixed depth impairs the comparability of different  
26 studies while associated uncertainty over the most appropriate definition limits the  
27 confirmability of studies utilising the mixed depths.

28 **Keywords:** mixed depth, lake, phytoplankton, oxygen, euphotic depth

## 29 1. Introduction

30 The “mixed layer” of a lake is a physical concept referring to a layer at the surface of a lake  
31 within which temperature is uniform (Robertson and Imberger, 1994; Sverdrup, 1953)  
32 (Fig.1a). The depth of the mixed layer, or epilimnion, depends on the balance between  
33 stratifying and mixing forces, with deepening being driven by wind mixing and convective  
34 cooling and shallowing being driven by warming (Wüest and Lorke, 2003). In stratified  
35 lakes, this layer typically overlies water in which the mixing rates are significantly smaller,  
36 enabling vertical gradients to develop in variables of interest, including temperature,  
37 particulate matter and dissolved gasses. This concept is used extensively and underpins our  
38 understanding of limnological processes. It is therefore fundamental for monitoring and  
39 assessment purposes (Jaša et al., 2019; Peter et al., 2009; Schauser et al., 2003) and studies on  
40 the restoration of lakes (Hoyer et al., 2015; Hupfer et al., 2016; Stroom and Kardinaal, 2016)  
41 as well as the limnology of lakes (Brainerd and Gregg, 1995; Diehl, 2002; Wüest and Lorke,  
42 2003).

43 There are, though, many practical problems generated by the concept of an idealised mixed  
44 depth. The layer is mixed by turbulence, but turbulence itself is not commonly measured  
45 directly. Furthermore, where turbulence has been directly measured it has shown the actively  
46 mixing layer can be substantially shallower than the isothermal layer (MacIntyre, 1993;  
47 Tedford et al., 2014). These measurements have indicated that temperature differences as  
48 little as 0.02 °C can delineate regions with different mixing rates (MacIntyre, 1993). The  
49 “mixed layer” can therefore be sub-divided into two regions; an actively mixed upper layer  
50 and a region below whose depth is determined by recent mixing, and characterised as  
51 “mixed” by its homogeneity in terms of one or more variables, most commonly temperature  
52 or density (Brainerd and Gregg, 1995). As temperatures are frequently only measured to an  
53 accuracy of 0.1 or 0.2 °C, and at only 0.5 m or 1 m vertical resolution or less, the most

54 commonly collected limnological temperature profiles cannot identify this actively mixing  
55 layer. It is even questionable whether this depth of recent mixing can be accurately  
56 determined using relatively coarse resolution measurements, as sharp changes in gradient can  
57 become smeared, blurring the boundary between epilimnion and metalimnion. Furthermore,  
58 temperature profiles can be complicated by the presence of secondary thermoclines  
59 developing during the daytime, enhancing the potential for confounding results arising from  
60 different mixed depth definitions. Such diurnal thermoclines can affect gas fluxes (MacIntyre  
61 et al., 2002) and the vertical distribution of nutrients and phytoplankton (MacIntyre and  
62 Melack, 1995). These secondary thermoclines can complicate the estimation of a  
63 systematically defined mixed depth. Each ecological variable is also subject to different  
64 source and sink terms operating at different timescales. Thus, physical mixing within the  
65 epilimnion might be sufficient for homogenising a variable with slow rates of production or  
66 loss, but the same mixing may be insufficient for homogenising a variable with faster  
67 production and loss.

68 The necessity to infer the mixed depth without direct turbulence measurements has led to a  
69 vast array of methods being developed for defining the depth of the mixed layer, typically  
70 exploiting the notion of a vertical limnological profile being generated by rapid vertical  
71 mixing in the surface waters of a lake and much diminished mixing beneath. A Web of  
72 Science search using terms 'lake' AND 'mix\* depth' AND 'layer' followed by removal of  
73 non-lake references or those referring to sediment mixed depths or chemoclines identified at  
74 least 313 research papers explicitly referring to a mixed layer. Often references to the mixed  
75 depth were descriptive (24 %) or theoretical (16 %) rather than quantitative and in 10 % of  
76 papers the mixed depth was arbitrarily or visually defined. The remaining studies determined  
77 the mixed depth using a variety of methods which included being calculated within lake  
78 models (11 %), fixed within mesocosm or laboratory experiments (8 %), directly measured

79 through turbulence (8 %) or calculated using a secondary variable (23 %). The latter method  
80 could be categorised into temperature (Coloso et al., 2008) or density gradients (Staeher et al.,  
81 2012), temperature (Wilhelm and Adrian, 2007), or density differences (Winder et al., 2009)  
82 and isotopic (Imboden et al., 1983) or chemical tracers (Maiss et al., 1994). Temperature  
83 gradients were most commonly used to define the mixed depth, followed by density  
84 gradients, temperature thresholds and density thresholds. There are, however, at least 20  
85 different thresholds and gradients of temperature or density currently being applied to  
86 estimate the mixed depth (Table 1).

87 Implicitly, the common usage of such a wide variety of methods suggests that each one is  
88 assumed to define approximately the same depth of mixed layer. If the vertical profiles of a  
89 lake match the idealised concept, then this should be true, but any discrepancies from an  
90 idealised profile could lead to different methods producing different estimates for the mixed  
91 depth. This would make a cross comparison of mixed layer depths between different studies  
92 meaningless and poses difficulties for the understanding and quantification of linkages to  
93 biological or chemical processes.

94 These methodological caveats are of particular concern when using the mixed depth as an  
95 explanatory or predictive variable in chemical and ecological studies. For example, the mixed  
96 depth can control the vertical distribution of phytoplankton and therefore the light climate to  
97 which they are exposed (Diehl et al., 2002). The ability for a phytoplankton community to  
98 grow and maintain biomass depends on the ratio of the mixed depth to the euphotic depth  
99 (Huisman, van Oostveen, & Weissing, 1999) in addition to the loss of cells due to sinking  
100 and the motility and light affinity of the species in the community (Diehl et al., 2002;  
101 Huisman et al., 2002; Jäger et al., 2008). Mixing that encroaches into the hypolimnion during  
102 stratification can also incorporate nutrients into the mixed layer increasing their availability  
103 for phytoplankton near the surface (Kunz and Diehl, 2003) and mix oxygen into the

104 hypolimnion potentially reducing future internal loading (Mackay et al., 2014). Having a  
105 robust estimate of mixing is therefore required to understand the vertical positioning and  
106 composition of phytoplankton taxa within a lake, along with the mechanisms of bloom  
107 formation (Cyr, 2017) and the associated water quality impacts (Dokulil and Teubner, 2000;  
108 Jaša et al., 2019).

109 Similarly, the vertical pattern of productivity in the water column is influenced by the mixed  
110 depth and water clarity (Obrador et al., 2014); therefore lake metabolism studies require a  
111 robust mixed depth estimation. The depth of surface mixing determines how much of the  
112 water column has regular contact with the atmosphere, influencing the depth of oxygen  
113 penetration. This is particularly important in stratified, productive systems where incomplete  
114 mixing can result in anoxia in the hypolimnion due to the oxidisation of organic matter by  
115 bacteria (Nürnberg, 1995). The direction of the flux of oxygen into and out of the mixed layer  
116 will also vary depending on the vertical distribution of primary producers in the water column  
117 relative to the mixed depth (Obrador et al., 2014; Peeters et al., 2016; Staehr et al., 2012,  
118 2010).

119 Despite the widespread use of the mixed depth concept and the large number of methods used  
120 to estimate mixed depth, there is a lack of research evaluating the consistency among  
121 methods of mixed depth estimation and the implications of using different estimates when  
122 interpreting ecological and chemical data. This study therefore aims to: (1) determine if  
123 different methods of calculating the mixed depth produce comparable estimates; (2) evaluate  
124 the extent to which ecological and chemical parameters are homogeneously distributed  
125 throughout the mixed depth; (3) evaluate how the choice of mixed depth definition may  
126 influence the calculation of simple example metrics relevant to studies of phytoplankton  
127 dynamics and metabolism. Analysis of vertical profiles of physical, chemical and ecological

128 parameters collected from a small meso-eutrophic lake in the UK were used to address these  
129 aims.

130 **2. Materials and methods**

131 *2.1. Site description*

132 Blelham Tarn is a small (surface area 0.1 km<sup>2</sup>), moderate depth lake (mean depth 6.8 m,  
133 maximum depth 14.5 m) (Ramsbottom, 1976), which stratifies typically for seven to eight  
134 months each year between spring and autumn. It is located in north-west England, UK  
135 (54°24'N, 2°58'W) and lies on the meso-eutrophic boundary (mean total phosphorus 24.5  
136 mg m<sup>-3</sup>) (Maberly et al., 2016).

137 *2.2. Field methods and data collection*

138 Vertical profiles of oxygen, chlorophyll *a* (measured via fluorescence as a proxy for  
139 phytoplankton biomass), temperature, specific conductivity and pH were measured using a  
140 YSI EXO2 multi-parameter sonde. Given the limitations of chlorophyll *a* fluorescence  
141 profiles (Gregor and Maršálek, 2004), water samples for chemical determination of  
142 chlorophyll *a* were taken at metre intervals in the water column (1-10 m) using standard  
143 methods (Mackereth et al., 1979). Vertical profiles of chlorophyll *a* obtained using both  
144 methods were compared visually and statistically using linear regression ( $R^2=0.53$ ,  $p<0.001$ ).  
145 The probes were calibrated every six weeks according to manufacturer specifications.  
146 Profiles were measured weekly between 9:30 am and 11 am during the stratified period (46  
147 sample days), defined here as when the density difference from the surface to the bottom was  
148 greater than 0.1 kg m<sup>-3</sup>, at 0.5 m intervals in the water column from 1 m to 13 m (2016) and  
149 0.5 m to 13 m (2017).

150 A LI-COR underwater quantum cos-corrected sensor was also used to measure  
151 photosynthetically active radiation (PAR); measurements were taken just below the surface  
152 and then at one-metre intervals from 1 m to 9 m. The natural logarithm of the PAR  
153 measurements were regressed with depth and the slope of the equation was used to estimate



154 the extinction coefficient ( $k$ ) for each sample day. The euphotic depth ( $z_{eu}$ ) was then defined  
155 as the depth where only 1 % of the surface measurement of PAR remained:

$$156 \quad z_{eu} = \ln(100) / k \quad (1)$$

157

### 158 *2.3. Methods for estimating mixed depth, $z_{mix}$*

159 Four methods of mixed depth estimation were tested for consistency, the first two methods  
160 used threshold changes in density (Method 1a) and temperature (Method 1b) from surface  
161 values to determine the depth of the mixed layer whereas Methods 2 and 3 determined the  
162 depth of the mixed layer statistically.

#### 163 *2.3.1. Method 1a: Density threshold*

164 The baseline mixed depth for this study was calculated as the depth at which the density first  
165 became  $0.1 \text{ kg m}^{-3}$  greater than the density at the surface (e.g. Andersen et al., 2017) (Fig.1b).  
166 Water density was calculated using water temperature and salinity from equations within  
167 Lake Analyzer (Read et al., 2011). Salinity was calculated from conductivity using the  
168 GibbsSeaWater (GSW) Oceanographic Toolbox (McDougall and Barker, 2011).

#### 169 *2.3.2. Method 1b: Temperature threshold*

170 Temperature is frequently used instead of density to define the mixed layer, therefore a  $1 \text{ }^\circ\text{C}$   
171 difference in temperature from the surface was used, roughly equating to a  $0.1 \text{ kg m}^{-3}$  density  
172 difference at moderate water temperatures. Below these temperatures the density difference  
173 will be smaller and vice versa for higher temperatures (Fig.1b).

174 Equivalent and directly comparable threshold methods cannot be applied to chemical and  
175 ecological variables due to their different units of measure. Therefore, two statistical methods  
176 were used which avoid the use of an arbitrary threshold or gradient and could therefore be

177 applied to profiles of chlorophyll *a* fluorescence, oxygen, pH and specific conductivity, as  
178 well as density profiles. If the idealised concept of the stereotypical shape of the vertical  
179 density profile holds true then both these statistical methods should provide estimates of  
180 mixed depth which are reasonably consistent with each other and with the mixed depth  
181 estimated by a density threshold (Fig. 1). Similarly, if the epilimnion is truly mixed then  
182 applying these methods to other limnological variables should also estimate a comparable  
183 depth for the bottom of the mixed layer.

184 *2.3.3. Method 2: Intersection of the plane of maximum gradient with the plane of the profile*  
185 *minimum (or maximum)*

186 A Generalised Additive Model (GAM) with a gamma error distribution and logarithm link  
187 function was fitted to every profile for each variable collected (46 sample days, 6 variables =  
188 276 profiles in total) using the mgcv package (version 1.8-26) (Wood, 2011) within the R  
189 programming language (R Core Team, 2018). The number of knots used in the GAM were  
190 optimized and fixed for each variable and the fitted values were predicted at 0.5 m depth  
191 intervals. Using the fitted predictions, the first derivative was calculated using forward  
192 differences to find the depth of the maximum gradient. At the depth of the maximum gradient  
193 the plane was extrapolated to all depths using the intercept and slope. Vertical lines were then  
194 drawn corresponding to the mean of three maximum and minimum values from each profile.  
195 The depth where the vertical lines intersected the extended maximum gradient line marked  
196 the top and bottom of the thermocline, or equivalent for other variables, that is, the mixed  
197 layer depth and the top of the hypolimnion, respectively (Fig. 1c).

198 *2.3.4. Method 3: Depth of statistically significant deviation*

199 Using the confidence intervals from the first derivative of the fitted GAM, the sections of the  
200 profile where changes in the gradient were significantly different from zero were calculated

201 (Simpson, 2018). The section of the profile that contained the depth of the maximum  
202 gradient was identified, with the upper and lower values of this section being the mixed depth  
203 and the top of the hypolimnion, respectively (Fig.1d).

#### 204 *2.4. Comparison of mixed depth method estimations*

205 To compare the differences in mixed depth estimates, the mean difference (including the  
206 directional sign of the difference i.e. shallower or deeper), mean absolute difference (not  
207 including the directional sign), root mean square error and the range were calculated for the  
208 different estimates of mixed depth for each sample day. The relative shift in the mixed depth  
209 (shallowing, deepening or no change) was calculated between sample days as well as the  
210 percentage of instances in which the methods were consistent. Initial comparisons were made  
211 between temperature and density thresholds (Methods 1a and 1b), followed by comparing  
212 Method 1a with the two statistical methods (Methods 2 and 3).

213 Statistical models were then used to determine if the depth of the mixed layer calculated from  
214 density using Method 2 was a good predictor for the depth of the mixed layer calculated by  
215 Method 2 from the other variables. A similar assessment was carried out using Method 3.  
216 This was initially assessed by linear regression of the density-derived mixed depth against the  
217 depth of the mixed layer derived from chlorophyll *a*, oxygen, pH and specific conductivity  
218 profiles. The residuals from each regression were visually inspected for normality,  
219 homoscedasticity, autocorrelation, and the influence of outliers with no issues found. Non-  
220 linearity was initially assessed visually and then each model was fitted with a quadratic  
221 density-derived mixed depth term to optimise the model fit. The density-derived mixed depth  
222 as a predictor of the mixed depth calculated from oxygen and specific conductivity profiles  
223 was better described using a quadratic model whereas the equivalent for chlorophyll *a* and pH  
224 were best described using a linear model based on the *F*-test.

225 *2.5. Determining the homogeneity of ecological and chemical parameters within the mixed*  
226 *depth*

227 The coefficient of variation (expressed as a percentage) and the range of values for  
228 temperature, chlorophyll *a*, oxygen, specific conductivity and pH within the mixed layer were  
229 calculated for each method of mixed depth estimation and compared to the equivalent  
230 variation for the whole water column.

231 *2.6. Calculation of example metrics using different mixed depth estimates*

232 The following metrics were calculated for each sample day using mixed depth estimates for  
233 Method 1a, Method 2 and Method 3: (a) the percentage of oxygen and chlorophyll *a* within  
234 the mixed layer and whether more than 50% of chlorophyll *a* and oxygen were contained  
235 within the mixed layer, (b) the directional flux of oxygen, that is, the sign of the difference in  
236 the mean concentration of oxygen in the mixed layer compared to the concentration 0.5 m  
237 below and, (c) the ratio between the mixed depth and euphotic depth.

238 **3. Results**

239 *3.1. Comparing mixed depth estimates*

240 *3.1.1. Methods 1a and 1b*

241 Mixed depth estimates calculated using temperature were on average 0.7 m deeper than  
242 estimates calculated from the density baseline, equivalent to an increase of 70 %. The RMSE  
243 was 1.1 m. The differences differed temporally (Fig.2) with the maximum daily range in  
244 values being 5.5 m.

245 *3.1.2. Methods 1a, 2 and 3*

246 There were large differences between the density-derived estimates of mixed depth calculated  
247 using the three different methods (Fig. 3). Method 2 estimates were shallower than Method  
248 1a by 0.8 m on average, whereas Method 3 estimates were deeper by 0.6 m (Table 2). The

249 daily differences in the estimates had no consistent systematic pattern (Fig. 3), with the  
250 largest daily range in values (5 m) occurring between Method 1a and Method 2. The methods  
251 were also inconsistent on whether there was shallowing, deepening or no change in the mixed  
252 depth between sample days with methods only being directionally consistent for 51 % of  
253 sample days (one method disagreed for 42 % of sample days and three different answers  
254 occurred for 7 % of sample days).

### 255 *3.2. Using the density-derived estimate as a predictor for ecological and chemical derived* 256 *estimates of mixed depth*

257 Mixed depths calculated using ecological and chemical parameters were varied and dissimilar  
258 from the estimates calculated from density (Fig. 4). The density-derived estimate was found  
259 to be a poor predictor for the estimates using chlorophyll *a*, pH and specific conductivity  
260 profiles, with low *F*-statistic values and weak or insignificant  $r^2$  and *p*-values (Table 3). A  
261 significant relationship was found between the depth of the oxygen derived mixed depth and  
262 the density derived mixed depth using a quadratic model. Further statistical testing, however,  
263 demonstrated that at depths shallower than 4.5 m the density derived mixed depth was a poor  
264 predictor for the equivalent oxygen derived mixed depth.

265 Mixed depth estimates were also a poor predictor of the chlorophyll *a* maxima for 2016 and  
266 2017 and a good predictor for the depth of the oxygen maxima during 2016 using Method 3  
267 but not during 2017 when no significance was found (Table 3).

### 268 *3.4. Determining the homogeneity of limnological variables within the mixed layer*

269 As expected, temperature had a small coefficient of variation and range of values within the  
270 mixed layer compared to the whole water column suggesting a homogenous distribution of  
271 heat within the mixed layer (Fig. 5; Table 4). The coefficient of variation and range of values  
272 in the mixed layer for specific conductivity were also small relative to the whole water

273 column suggesting homogeneity (Fig. 5; Table 4). Though the coefficient of variation was  
274 relatively low for oxygen in the mixed layer, values could differ by up to 2.4 mg/L at times  
275 suggesting that oxygen concentrations were not always homogenous (Fig. 5; Table 4).  
276 Chlorophyll *a* and the concentration of hydrogen ions demonstrated the largest coefficients of  
277 variation and range of values in the mixed layer relative to the water column (Table 4) and  
278 therefore had a heterogeneous distribution in the mixed layer for much of the stratified period  
279 (Fig.5).

### 280 *3.5. The impact of using different mixed depth estimates when calculating example metrics*

#### 281 *3.5.1. The percentage of chlorophyll *a* and oxygen within the mixed layer*

282 The mean percentage of chlorophyll *a* in the mixed layer during the stratified period differed  
283 between methods. Even the proportion of days when the majority (>50 %) of chlorophyll *a*  
284 was contained within the mixed layer varied greatly depending upon the mixed layer  
285 estimation method (Fig 6). For 2016 the proportion of days when the majority of chlorophyll  
286 *a* was contained within the mixed layer was 35 %, 74 % and 39 % for Methods 1a, 2 and 3  
287 respectively, whereas for 2017 the values were 48 %, 65 % and 30 %. The methods only all  
288 agreed for 50 % of sampling days on whether the majority of chlorophyll *a* was contained  
289 within the mixed layer (Fig.6).

290 The mean percentage of oxygen in the mixed layer for the whole of the stratified period also  
291 differed depending on the definition used for mixed depth (Fig. 6). The proportion of days  
292 when the percentage of oxygen in the mixed layer was greater than 50 % varied between  
293 methods (Fig. 6). For 2016 the proportion of days when the majority of oxygen was  
294 contained within the mixed layer was 43 %, 83 %, and 43 % for Methods 1a, 2 and 3  
295 respectively whereas for 2017 the values were 61 %, 74 % and 35 %. The methods all agreed

296 on whether the majority of oxygen in the water column was in the mixed layer for less than  
297 half (46 %) of the sampling days (Fig.6).

### 298 *3.5.2. The directional flux of oxygen*

299 The direction of the flux of oxygen between the mixed layer and the layer below, as  
300 determined by whether concentration was greater within or beneath the mixed layer, was not  
301 always consistent between methods with contradictory results occurring 24 % of the time  
302 (Fig.7). Even when the direction of the oxygen flux was consistent between methods the size  
303 of the gradient between the mixed layer and the water directly underneath was markedly  
304 different (Fig.7). Thus, both the direction and magnitude of the flux of oxygen between the  
305 mixed layer and the thermocline were highly dependent on how the mixed layer depth was  
306 defined.

### 307 *3.5.3. Mixed layer to euphotic layer depth ratio*

308 The ratio of mixed depth to euphotic depth was very different depending on which method  
309 was used to calculate mixed depth (Fig. 8). The mean ratio calculated using Method 2 (0.9)  
310 was typically greater than that using Method 1a (0.7), which was itself greater than that using  
311 Method 3 (0.6). As well as the systematic differences there was also a lot of temporal  
312 variation between the consistency of the estimates (Fig.8). The mean difference between the  
313 mixed depth to euphotic depth ratio between Method 1a and Method 2 was 0.32 and between  
314 Method 1a and Method 3 was 0.90, with methods being contradictory as to whether the  
315 euphotic or the mixed depth was deeper for 20 % of sample days (Fig. 8).

316

#### 317 **4. Discussion**

318 The results demonstrate that different approaches to mixed depth estimation are not  
319 necessarily comparable, even when those methods are underpinned by the same conceptual  
320 description of a mixed depth. This is the case when the same method is used with different  
321 variables (Fig. 4) or when different methods are used with the same variable (Fig. 3). It is  
322 particularly worth noting that, estimations of mixed depth from temperature profiles differ  
323 from estimations of mixed depth derived from density profiles (Fig. 2). This is partly due to  
324 the non-linear relationship between temperature and density and partly due to the deviation of  
325 observed density profiles from an idealised profile, such as when both diel and seasonal  
326 pycnoclines are present. The functional role density gradients have in influencing mixing  
327 rates suggests that density be preferred to temperature as a variable for defining mixing  
328 length scales, despite the frequency with which temperature is still used (Table 1). The  
329 number of methods and variables examined here for estimating mixed depth is a relatively  
330 small sample compared with the vast array of mixed depth definitions in the literature (Table  
331 1). Nevertheless, they indicate that even the direction of change in mixed depth over time can  
332 be dependent on the method chosen for its calculation. To some extent the development of  
333 automated tools for calculating mixed depth such as Lake Analyzer (Read et al., 2011), offers  
334 a means to reduce the proliferation of definitions.

335 It is not necessarily the case though, that, a single definition of mixed depth estimation is  
336 always appropriate, as different definitions might be better suited to different conditions or  
337 different ecological questions. An example is the variety of mixed layer definitions used in a  
338 study comparing depth-related oxygen metabolism across disparate lakes (Giling et al.,  
339 2017), where it was considered that no one definition was suitable for all the lakes. It may  
340 also be sometimes appropriate, depending on the purpose of the study, to adopt a definition  
341 using a different variable than density or temperature, as the occurrence of a homogenous



342 surface layer in one property does not guarantee that it will be homogenous in another  
343 property (Table 4, Fig. 5). Studies interested in identifying homogenous distributions of  
344 phytoplankton, for example, for which gradients of light and nutrients as well as turbulence  
345 are controlling their distribution (Huisman et al., 1999; Kunz and Diehl, 2003), could be  
346 inaccurate if a density definition of mixed layer was used. That the depth of the mixed layer  
347 is highly dependent on the definition, and that not all properties will be evenly distributed  
348 within it, necessitates caution when analysing vertically resolved limnological data. Even the  
349 analysis of simple metrics relating to the distribution of chlorophyll *a* and oxygen  
350 demonstrates that the choice of mixed depth definition could influence the interpretation of  
351 results (Fig. 6-8). Thus, where phytoplankton samples are integrated over the epilimnion for  
352 assessing water quality (Noges et al., 2010) the assessment could be influenced by the  
353 definition of mixed layer adopted. Similarly, whether phytoplankton maxima are within or  
354 beneath the mixed layer will depend on the definition chosen. The oxygen flux into and out  
355 of the mixed layer is important for metabolism studies (Obrador et al., 2014), but the  
356 magnitude of the oxygen gradient between layers, and therefore the magnitude and direction  
357 of the oxygen flux, is highly dependent on the definition of mixed depth (Fig. 7). Nutrient  
358 fluxes will be similarly dependent on definition, which may have consequences for water  
359 quality determination and restoration responses (Hupfer et al., 2016; Read et al., 2014;  
360 Schauser et al., 2003). In general, the accuracy of flux estimated will be limited without  
361 turbulence measurements. The widely used ratio of the mixed depth to euphotic depth was  
362 also dependent on the definition of mixed depth used (Fig. 9). This is consequential, when  
363 explaining the formation of sub-surface phytoplankton maxima, which are thought to occur in  
364 eutrophic systems when the euphotic depth is deeper than the mixed depth (Hamilton et al.,  
365 2010; Leach et al., 2018; Mellard et al., 2011).

366 The interrogation and interpretation of vertical profiles is a fundamental and burgeoning area  
367 of limnological study (Brentrup et al., 2016; Hamilton et al., 2010; Leach et al., 2018;  
368 Obrador et al., 2014) and will require careful consideration of how best to use mixed depth as  
369 a predictive or explanatory variable or as a determinant of water quality monitoring. One  
370 approach is to assess the impact of using different mixed depth estimates when analysing  
371 results. For example, the Giling et al., (2017) study on metabolism found that halving or  
372 doubling the threshold density gradient used to estimate the mixed depth changed the  
373 estimated thickness of the metalimnetic depth zone by 22 %. For the study, this inconsistency  
374 was deemed relatively insignificant to the findings, however the authors highlighted that this  
375 would become problematic when aggregating metabolic rates to the metalimnion and  
376 hypolimnion (Giling et al., 2017). Another approach is to examine systematically which  
377 method or methods are more consistently useful than others for approximating a mixed depth.

## 378 **5. Conclusions**

379 By testing three methods of mixed depth and using them to calculate simple ecological and  
380 chemical metrics this study has demonstrated that methods of mixed depth estimation are  
381 inconsistent and influence the interpretation of chemical and ecological results. Based on  
382 these findings we recommend that future studies should:

- 383 • Favour density over temperature for estimating the mixed depth
- 384 • Not assume homogeneity of other variables within the mixed layer
- 385 • Assess the sensitivity of the findings of the study to mixed depth definition or
- 386 • Examine several methods to choose the most consistent and useful method for the
- 387 study

388 Ultimately, any method adopted for estimating mixed depth from standard limnological data  
389 should be used cautiously and with awareness of the potential deviation of observed profiles  
390 from idealised ones.

391

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601 **Tables**

602 Table 1. Examples of temperature and density thresholds and gradients used in existing  
 603 literature to calculate the mixed layer depth.

| Reference                           | Method                                    |
|-------------------------------------|---|
| <i>Temperature thresholds</i>       |   |
| (Augusto-Silva and MacIntyre, 2019) | 0.02 °C from the surface                  |
| (Yang et al., 2018)                 | 0.2 °C from the surface                   |
| (Zhao et al., 2018)                 | 0.8 °C from the surface                   |
| (Mackay et al., 2011)               | 1 °C from the surface                     |
| (Vidal et al., 2010)                | 0.04 °C from the surface                  |
| <i>Temperature gradients</i>        |   |
| (Kasprzak et al., 2017)             | 1 °C m <sup>-1</sup>                      |
| (Coloso et al., 2008)               | 1 °C /0.5 m.                              |
| (Xie et al., 2017)                  | 0.01 °C m <sup>-1</sup>                   |
| (Yankova et al., 2016)              | 0.5 °C m <sup>-1</sup>                    |
| (Özkundakci et al., 2011)           | 0.25 °C m <sup>-1</sup>                   |
| (Hamilton et al., 2010)             | 0.225°C m <sup>-1</sup>                   |
| (McCullough et al., 2007)           | 0.05 °C m <sup>-1</sup>                   |
| (Whittington et al., 2007)          | 0.02 °C m <sup>-1</sup>                   |
| (Wilhelm and Adrian, 2007)          | Depth of the maximum temperature gradient |
| <i>Density thresholds</i>           |   |
| (Andersen et al., 2017)             | 0.1 kg m <sup>-3</sup> from the surface   |
| <i>Density gradients</i>            |   |

---

|                           |   |
|---------------------------|---|
| (Staeher et al., 2012)    | $0.07 \text{ kg m}^{-3} \text{ m}^{-1}$   |
| (Giling et al., 2017)     | $0.03 \text{ kg m}^{-3} \text{ m}^{-1} - 0.18 \text{ kg m}^{-3} \text{ m}^{-1}$ |
| (Tonetta et al., 2016)    | $0.03 \text{ kg m}^{-3} \text{ m}^{-1}$   |
| (Zwart et al., 2016)      | $0.1 \text{ kg m}^{-3} \text{ m}^{-1}$  |
| (Lamont and Laval, 2004.) | $0.5 \text{ kg m}^{-3} \text{ m}^{-1}$  |

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604

605

606 Table 2. The mean difference, root mean square error (RMSE) and range in mixed depth  
 607 estimates as calculated using Methods 1a, 1b, 2 & 3. Negative values indicate that the latter  
 608 mixed depth estimates are deeper.

|                                | M1a-M1b | M1a-M2 | M1a-M3 |
|--------------------------------|---------|--------|--------|
| Mean difference (m)            | 0.7     | 0.8    | -0.6   |
| Mean absolute difference (m)   | 0.7     | 1.2    | 1.3    |
| Mean percentage difference (%) | 70      | 108    | 77     |
| RMSE (m)                       | 1.1     | 1.7    | 1.6    |
| Range (m)                      | 5.5     | 5      | 4.5    |

609

610

611 Table 3. Statistical model coefficients and adjusted  $R^2$  values for the depth of the density-derived mixed depth compared with the mixed depth  
612 calculated from chlorophyll-*a*, oxygen, specific conductivity and pH as well as the depth of the chlorophyll *a* and oxygen maxima for Method 2  
613 and Method 3. The significance level is denoted as \*\*\* $p < 0.001$ ; \*\* $p < 0.01$ ; \* $p < 0.05$ ,  $\cdot p < 0.1$ , ns- not significant. Quadratic models were  
614 used for oxygen and specific conductivity whereas linear models were used for chlorophyll *a*, chlorophyll *a* maxima, oxygen maxima and pH,  
615 2016 n=23; 2017 n=23.

|                             | 2016        |      |                     |       | 2017           |       |                 |     |             |      |                     |      |                |       |                 |     |
|-----------------------------|-------------|------|---------------------|-------|----------------|-------|-----------------|-----|-------------|------|---------------------|------|----------------|-------|-----------------|-----|
|                             | Residual SE |      | <i>F</i> -statistic |       | Adjusted $R^2$ |       | <i>p</i> -value |     | Residual SE |      | <i>F</i> -statistic |      | Adjusted $R^2$ |       | <i>p</i> -value |     |
|                             | M2          | M3   | M2                  | M3    | M2             | M3    | M2              | M3  | M2          | M3   | M2                  | M3   | M2             | M3    | M2              | M3  |
| Chlorophyll <i>a</i>        | 1.57        | 1.58 | 1.50                | 4.64  | 0.02           | 0.14  | ns              | *   | 0.88        | 1.07 | 20.74               | 1.00 | 0.47           | <0.01 | ***             | ns  |
| Oxygen                      | 0.93        | 0.99 | 31.57               | 23.33 | 0.74           | 0.67  | ***             | *** | 1.24        | 1.57 | 11.61               | 6.16 | 0.49           | 0.38  | ***             | *** |
| pH                          | 1.25        | 1.45 | 1.84                | 7.29  | 0.04           | 0.26  | ns              | ns  | 0.75        | 1.27 | 18.18               | 4.67 | 0.44           | 0.14  | ***             | ns  |
| Specific Conductivity       | 2.07        | 2.23 | 1.46                | 1.17  | 0.04           | 0.02  | ns              | ns  | 2.51        | 2.47 | 2.2                 | 1.07 | 0.1            | <0.01 | ns              | ns  |
| Chlorophyll <i>a</i> maxima | 1.71        | 1.23 | 0.20                | 0.92  | -0.04          | <0.01 | ns              | ns  | 2.02        | 0.96 | 0.02                | 1.04 | -0.05          | <0.01 | ns              | ns  |
| Oxygen maxima               | 1.59        | 1.46 | 3.77                | 15.87 | 0.11           | 0.40  | .               | *** | 2.02        | 1.22 | 0.03                | 0.28 | -0.05          | -0.03 | ns              | ns  |

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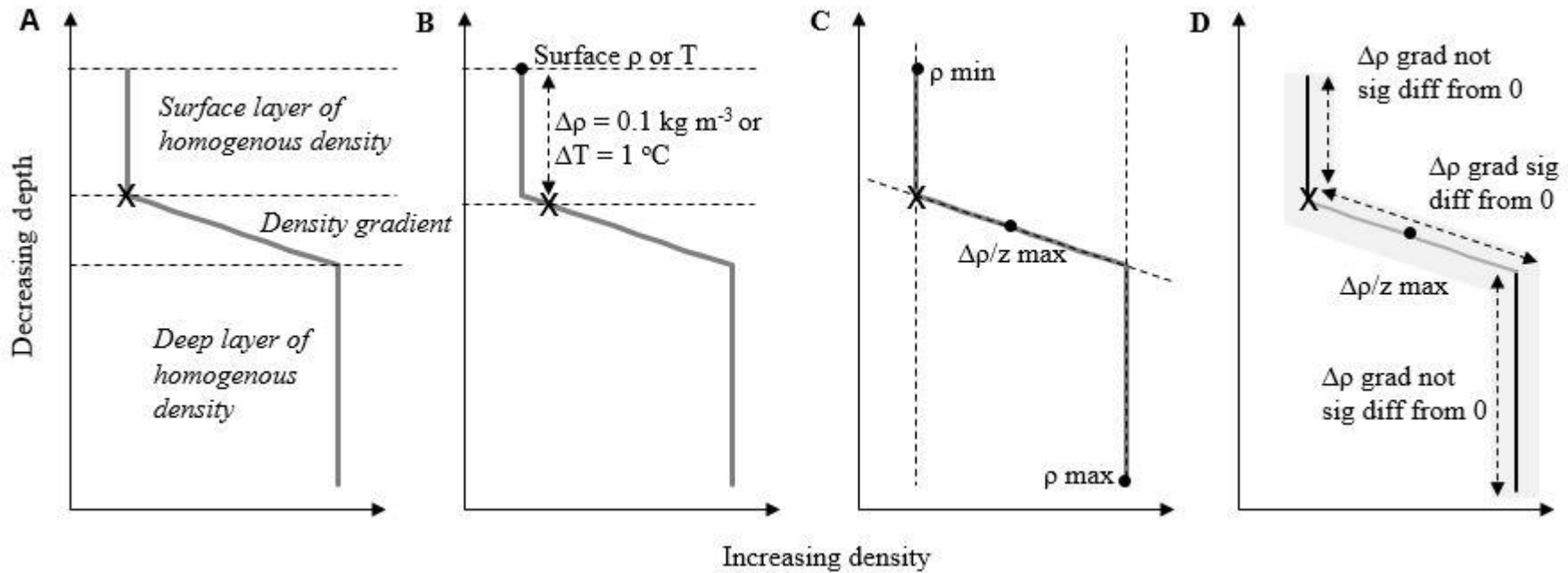
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618 Table 4. The coefficient of variation (COV) and the range of temperature, oxygen, chlorophyll *a*, concentration of hydrogen ions (exponential of  
619 pH) and specific conductivity values in the water column (WC) and the mixed layer for Method 1a (M1a), Method 2 (M2) and Method 3 (M3),  
620 percentage values in brackets depict the percentage variation in the mixed layer relative to the whole water column variation.

| <i>Variable</i>                            | <i>Mean coefficient of variation (COV) (%)</i> |             |             |             | <i>Mean Range</i> |              |               |              |
|--|--|-------------|-------------|-------------|-------------------|--------------|---------------|--------------|
|  | WC   | M1a         | M2          | M3          | WC                | M1a          | M2            | M3           |
| Temperature (°C)                           | 24.7   | 1.7 (7 %)   | 2.1 (9 %)   | 0.6 (2 %)   | 7.1               | 0.7 (10 %)   | 0.9 (13 %)    | 0.2 (3 %)    |
| Oxygen (mg L <sup>-1</sup> )               | 94.7   | 9.0 (10 %)  | 9.4 (10 %)  | 5.3 (6 %)   | 8.8               | 2.3 (26 %)   | 2.4 (27 %)    | 1.3 (15 %)   |
| Chlorophyll <i>a</i> (mg m <sup>-3</sup> ) | 74   | 17.1 (23 %) | 24.5 (33 %) | 11.6 (16 %) | 19.7              | 8.2 (42 %)   | 11.4 (58%)    | 5.3 (27 %)   |
| pH   | 48.7   | 16.2 (33 %) | 20.2 (42 %) | 11.8 (24 %) | 1778.2            | 950.3 (53 %) | 1073.6 (60 %) | 641.0 (36 %) |
| Specific Conductivity                      | 8.7  | 1.1 (13 %)  | 0.9 (10 %)  | 0.4 (5 %)   | 28.1              | 3.3 (12 %)   | 2.5 (9 %)     | 1.2 (4 %)    |

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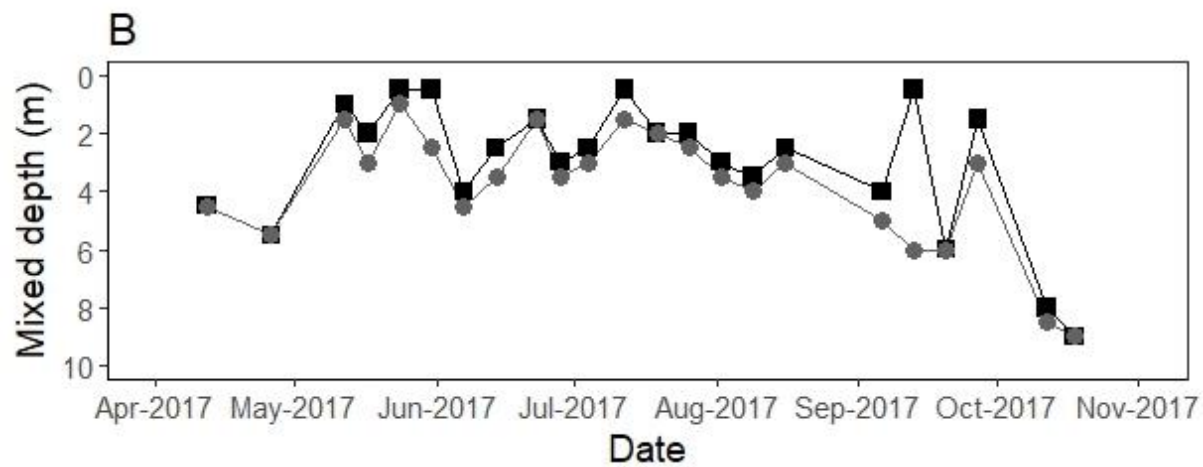
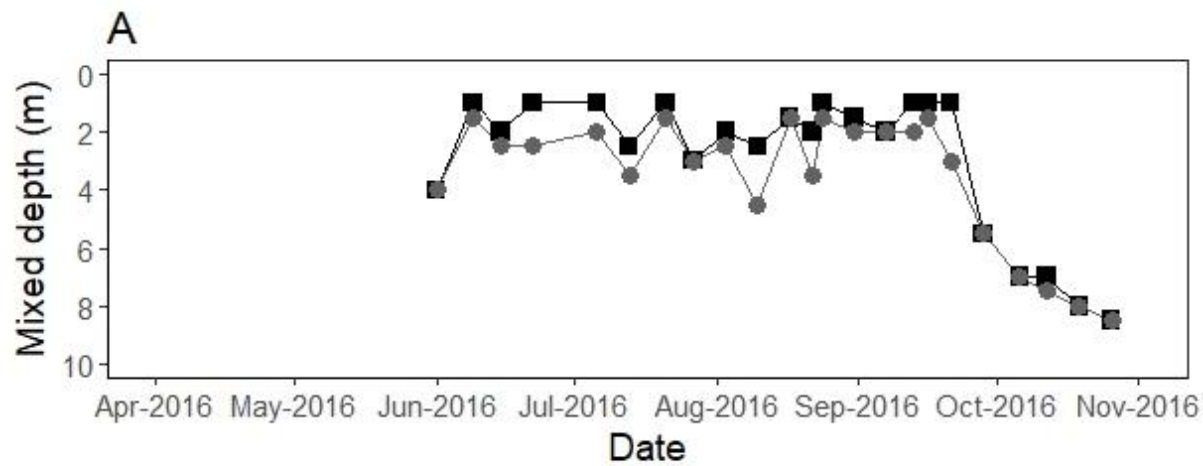
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627 Figure 1. Diagram of density profiles marking the mixed depth (X) for (a) a theoretical mixed depth; (b) estimating the mixed depth using a 0.1  
 628  $\text{kg m}^{-3}$  or  $1 \text{ }^\circ\text{C}$  difference from the surface (Surface  $\rho$  or T) (Methods 1a and b); (c) estimating the mixed depth using Method 2 where lines are  
 629 extended from the depth of the maximum gradient ( $\Delta\rho/\Delta z$  max), the density minimum ( $\rho$  min) and the density maximum ( $\rho$  max) with the upper  
 630 intersection of the lines marking the top of the pycnocline or base of the mixed depth and (d) estimating the mixed depth using Method 3 where  
 631 the upper and lower values of the section of the profile containing the depth of the maximum gradient ( $\Delta\rho/\Delta z$  max) and a change in the density  
 632 gradient ( $\Delta\rho$  grad) significantly different from zero marking the mixed depth and the top of the hypolimnion, respectively, the grey shading  
 633 marks the profile confidence intervals.

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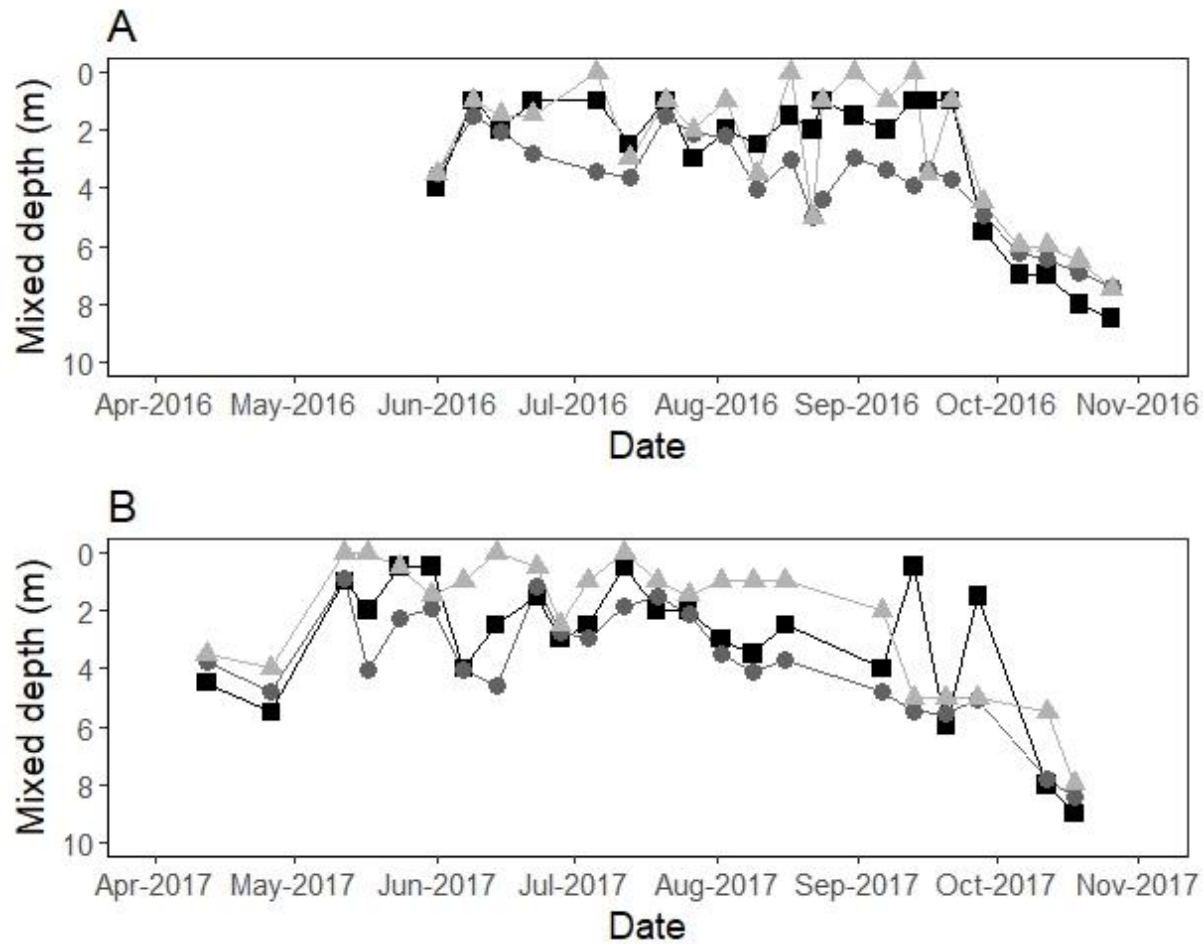
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639 Figure 2. Mixed depth estimates using Method 1a (density threshold; black square) and Method 1b (temperature threshold; grey diamond) in (a)  
 640 2016 and (b) 2017.

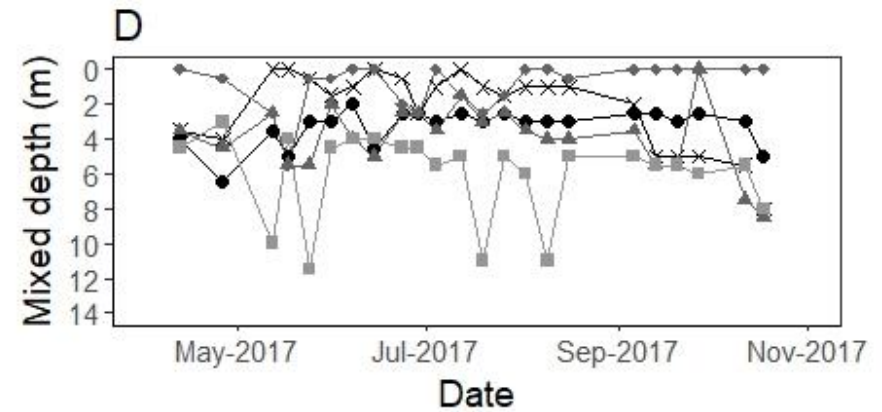
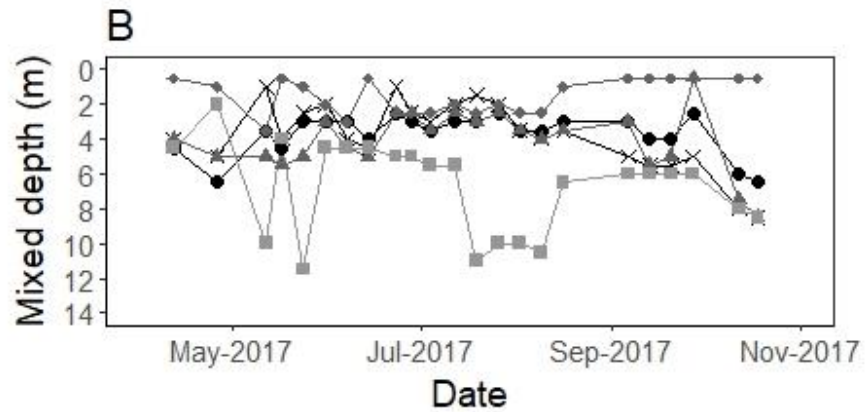
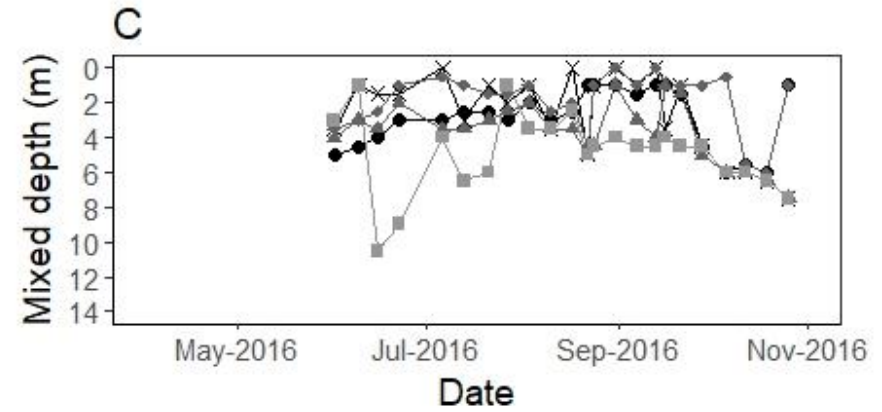
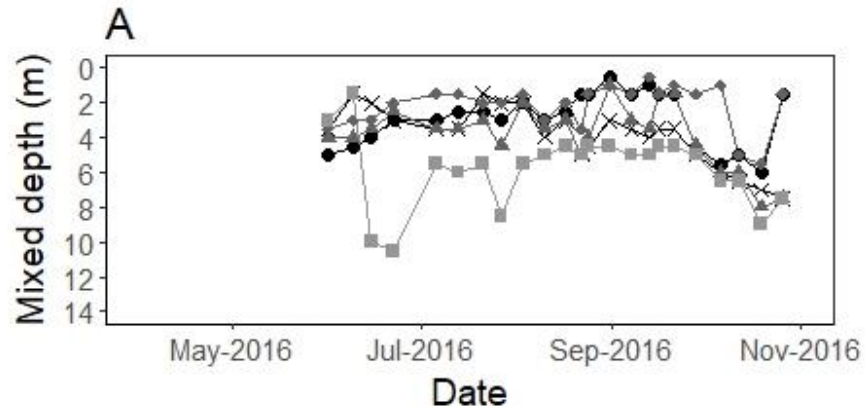
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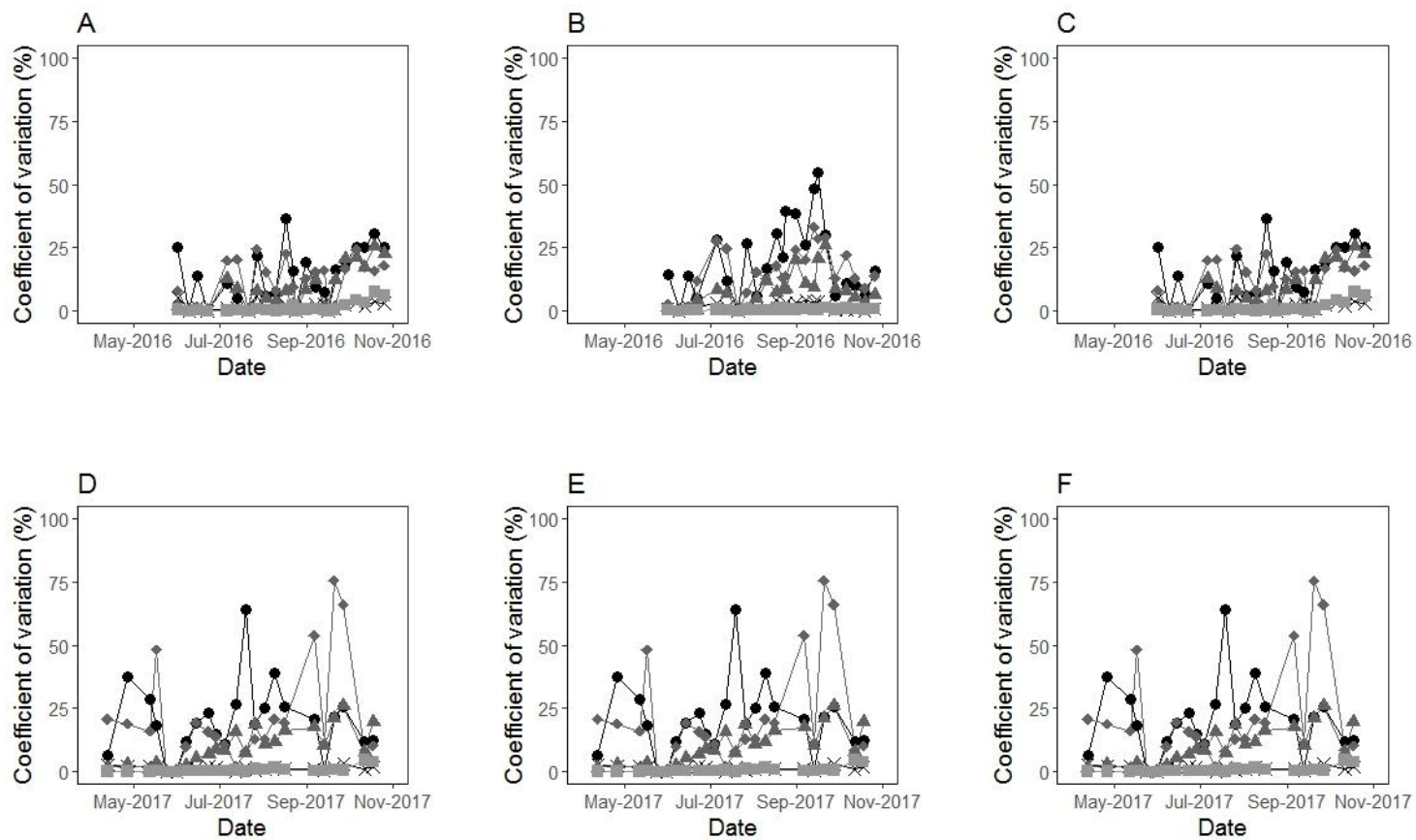
644 Figure 3. Density-derived mixed depth estimates using Method 1a (black square), Method 2 (grey circle) and Method 3 (light grey triangle) (a)  
645 2016 and (b) 2017.



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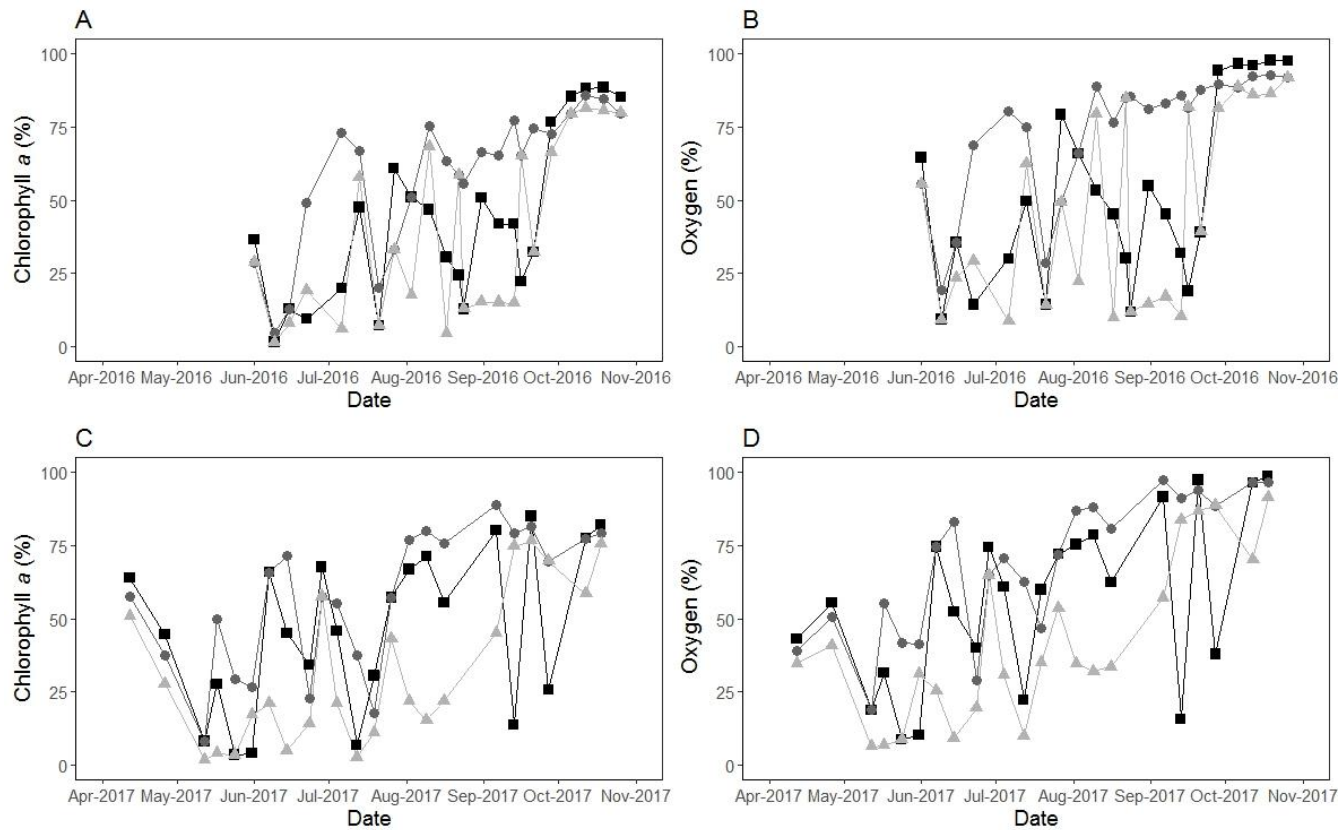
649 Figure 4. Depth of the mixed layer calculated from density ( ✱ ), chlorophyll-*a* ( ● ), oxygen ( ▲ ), pH ( ◆ ) and specific  
 650 conductivity ( ■ ) for (a) 2016 using Method 2, (b) 2016 Method 3 (c) 2017 Method 2 and (d) 2017 Method 3.



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652 Figure 5. The coefficient of variation in the mixed layer for temperature (  $\times$  ), chlorophyll *a* (  $\bullet$  ), oxygen (  $\blacktriangle$  ), concentration of  
 653 hydrogen ions (pH) (  $\blacklozenge$  ) and specific conductivity (  $\blacksquare$  ) for (a) 2016 Method 1a, (b) 2016 Method 2 , (c) 2016 Method 3, (d) 2017  
 654 Method 1a, (e) 2017 Method 2 and (f) 2017 Method 3.

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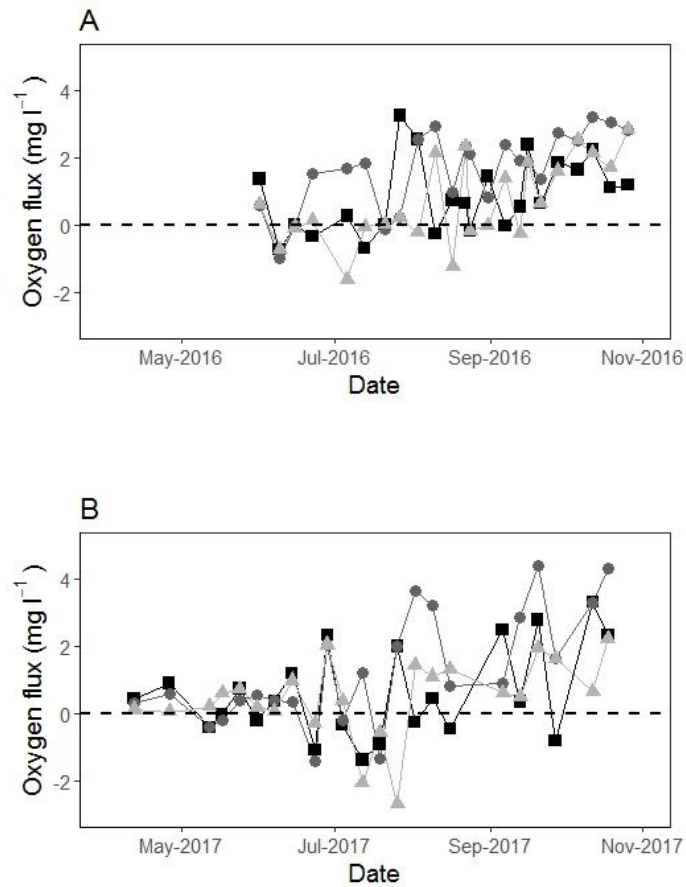
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657 Figure 6. The percentage of chlorophyll *a* and oxygen within the mixed layer using mixed depth estimates calculated using Method 1a (black  
 658 square), Method 2 (grey circle) and Method 3 (light grey triangle) for (a) chlorophyll *a* in 2016, (b) oxygen in 2016, (c) chlorophyll *a* in 2017  
 659 and (d) oxygen in 2017

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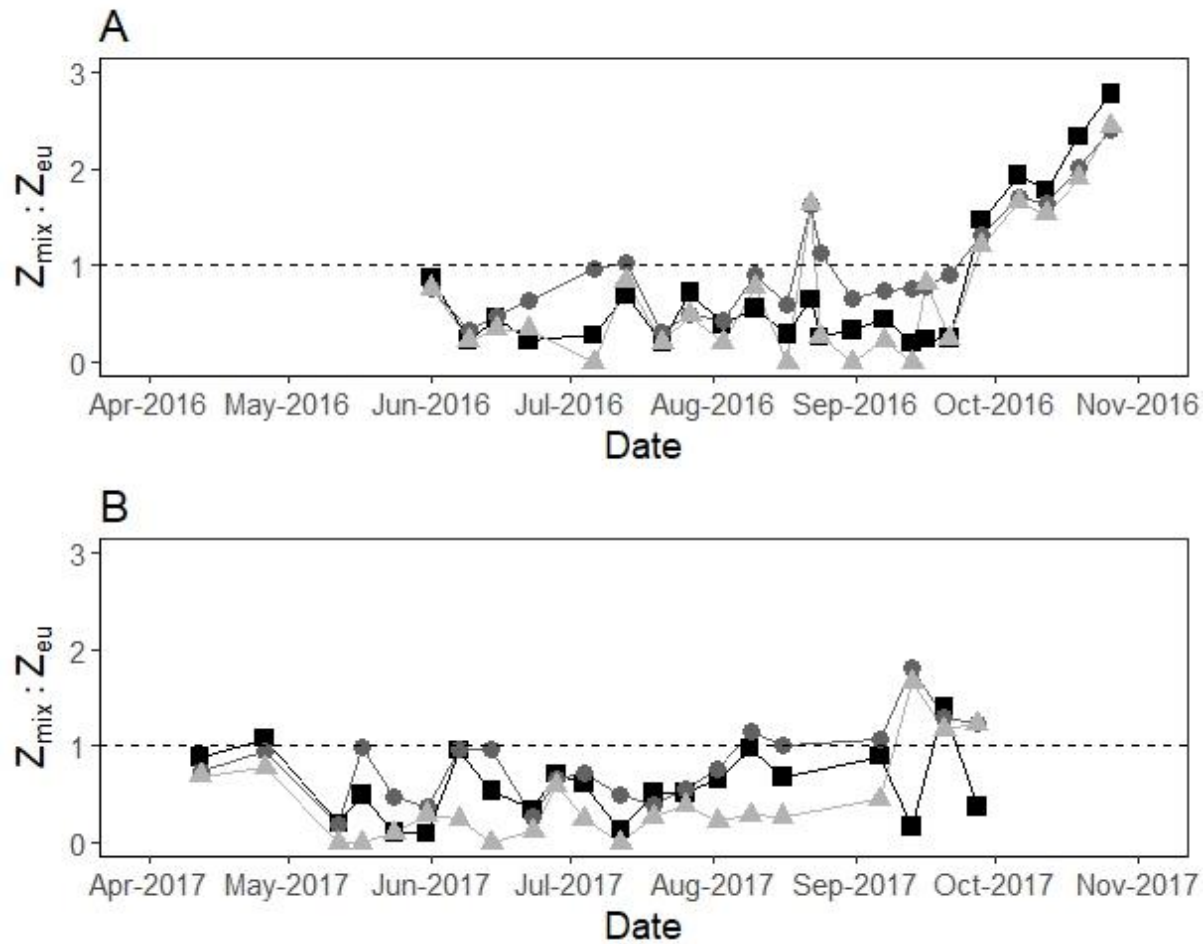


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664 Figure 7. The difference in the concentration of oxygen within the mixed layer compared to the concentration in the layer 0.5 m below using  
 665 mixed depth estimates calculated from Method 1a (black square), Method 2 (grey circle) and Method 3 (light grey triangle) for (a) 2016 and (b)  
 666 2017 .

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670 Figure 8. The  $z_{mix} : z_{eu}$  ratio calculated using density derived mixed depth estimated using Method 1a (black square), Method 2 (grey circle) and  
 671 Method 3 (light grey triangle) for (a) 2016 and (b) 2017. Values below the horizontal y intercept line at 1  $z_{mix} : z_{eu}$  mark when mixed depths are  
 672 shallower than the euphotic depth and vice versa for values above.