

Validating a notch filter for detection of targets at sea with ALOS-PALSAR data: Tokyo Bay

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Abstract

1
2 The surveillance of maritime areas is a major topic for security aimed at fighting issues as illegal traffick-
3 ing, illegal fishing, piracy, etc. In this context, Synthetic Aperture Radar (SAR) has proven to be particularly
4 beneficial due to its all-weather and night time acquisition capabilities. Moreover, the recent generation of
5 satellites can provide high quality images with high resolution and polarimetric capabilities. This paper is de-
6 voted to the validation of a recently developed ship detector, the Geometrical Perturbations Polarimetric Notch
7 Filter (GP-PNF) exploiting L-band polarimetric data. The algorithm is able to isolate the return coming from
8 the sea background and trigger a detection if a target with different polarimetric behavior is present. Moreover,
9 the algorithm is adaptive and is able to account for changes of sea clutter both in polarimetry and intensity. In
10 this work, the GP-PNF is tested and validated for the first time ever with L-band data, exploiting one ALOS-
11 PALSAR quad-pol dataset acquired on the 9th of October 2008 in Tokyo Bay. One of the motivations of the
12 analysis is also the attempt of testing the suitability of GP-PNF to be used with the new generations of L-band
13 satellites (e.g. ALOS-2). The acquisitions are accompanied by a ground truth performed with a video survey.

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14 A comparison with two other detectors is presented, one exploiting a single polarimetric channel and the other
15 considering quad-polarimetric data. Moreover, a test exploiting dual-polarimetric modes (HH/VV and HH/HV)
16 is performed. The GP-PNF shows the capability to detect targets presenting pixel intensity smaller than the
17 surrounding sea clutter in some polarimetric channels. Finally, the quad-polarimetric GP-PNF outperformed in
18 some situations the other two detectors.

19

Keywords

20 Synthetic Aperture Radar, Radar Polarimetry, Ship detection, ALOS PALSAR, notch filter.

21

I. INTRODUCTION

22 This paper addresses ship detection with Polarimetric Synthetic Aperture Radar (PolSAR).
23 Specifically a recent methodology proposed by the authors [1], [2], [3], [4] will be tested for
24 the first time ever with L-band data (i.e. quad-polarimetric ALOS-PALSAR).

25 SAR provides an attractive combination of high resolution images acquired from space
26 with relatively large swath width, night-time and all-weather capabilities [5], [6], [7], [8],
27 [9], [10]. An introduction on SAR is outside the purposes of this paper and the authors
28 redirect the readers to [11], [12], [13] for further details.

29 In SAR images, the main feature of a ship is a relatively large backscattering signal, which
30 is usually brighter in comparison to the sea background. The strength of the signal from a
31 vessel will be dependent on several factors, notably the size of the vessel and the material
32 from which it is made, where generally, the presence of metallic reflectors (triangular and
33 dihedral) will add to the overall brightness. For this reason, the intensity contrast was used
34 as a feature to discriminate between targets and sea clutter. Several methodologies were
35 proposed [6], [7], [8], [9], [10], [14], [15], [16], [17], [18], [19]. Most of these techniques
36 set a statistical test between the intensities of target and clutter background.

37 It is increasingly common for SAR satellites to have the capability to acquire data em-
38 ploying different antenna polarization configurations [20]. In order to provide the maximum
39 amount of information the phase of the backscattering needs to be recorded in addition to the
40 amplitude of the separate polarimetric channels. Examples of satellites with such capabilities
41 are ALOS-PALSAR, TerraSAR-X and RADARSAT-2.

42 For instance, the use of the cross-polarized channel (S_{HV}) instead than the co-polarized
43 ones (S_{HH} or S_{VV}) in dual-polarimetric acquisitions may increase substantially the detec-
44 tion performance [2], [6], [14], [15], [16], [17], [18], [19], [21], [22], [23], [24], [25], [26],
45 [27]. This is because the sea has a small scattering contribution in the cross-polarized chan-
46 nel, therefore improving the Signal to Clutter Ratio (SCR). One way to combine several
47 polarimetric channels is considering them as independent measurements and set a statistical
48 test on them [21], [22]. These first techniques showed large improvements compared to the
49 single polarization detectors. From the analysis provided by Liu et al. [22] and shared by
50 other authors [28], it was shown that the quad-polarimetric mode provides the best detection
51 performance, followed by the dual co-polarization combination S_{HH} and S_{VV} .

52 A second type of polarimetric ship detectors is based on physical scattering properties
53 of targets and ships [2], [23], [24], [25], [28] (some of them exploited the difference in
54 coherence or degree of polarization shown by ships and sea clutter. The technique presented
55 in this paper, namely Geometrical Perturbation - Polarimetric Notch Filter (GP-PNF) was
56 developed in [1], [2], [3] and evaluates the differences in the polarimetric signature between
57 the sea and targets.

58 This paper is focused on testing the GP-PNF on ALOS-PALSAR data. L-band may be
59 particularly valuable for ship detection considering the backscattering from sea clutter is
60 expected to be lower compared to C- or X-band. Therefore, L-band may possibly bring some

61 advantage over rough sea conditions or thin sea-ice. In the specific context of this paper, a test
 62 of the GP-PNF in L-band is necessary in order to verify the feasibility of using the algorithm
 63 at this frequency. The detection rule is based on the concept that the polarimetric behavior
 64 of targets and sea clutter remain separable. Considering the complexity of evaluating the
 65 interactions between the transmitted polarized wave and the objects on the scene, it is not
 66 trivial to state that vessels and sea will maintain a different polarimetric behavior that can
 67 be detected by the GP-PNF as they were observed to do in other frequencies (i.e. C- and
 68 X-band [1], [2], [3], [4]).

69 Additionally, the evaluation of the performance in L-band may be important in the context
 70 of the next JAXA mission ALOS-2, in order to understand if the GP-PNF can be employed
 71 with these data.

72 II. SHIP DETECTION WITH SAR POLARIMETRY

73 A. SAR polarimetry

74 The idea behind PolSAR is that the polarization of the electromagnetic (EM) wave can be
 75 exploited to extract information regarding the identity of the observed targets [20], [29], [30],
 76 [31], [32], [33]. Specifically, in order to characterize uniquely the behavior of a deterministic
 77 target, four observations (quad-pol) have to be carried out. These can be arranged in the
 78 *Scattering Matrix*:

$$[S] = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix}, \quad (1)$$

79 where H stands for a horizontally linear polarized wave, V for linear vertical, and the re-
 80 peated letter refers to transmitter-receiver. In the literature, a deterministic target that can be
 81 characterized by only one (deterministic) scattering matrix is often defined as *single* [29].

82 An equivalent representation is by a scattering vector:

$$\underline{k} = \frac{1}{2} \text{Trace}([S]\Psi_2) = [k_1, k_2, k_3, k_4]^T, \quad (2)$$

83 where $\text{Trace}(\cdot)$ is the sum of the diagonal elements of the matrix, T is for matrix transpose
 84 and Ψ_2 is a complete set of 2×2 basis matrices under a Hermitian inner product [29]. In
 85 the case of a reciprocal medium and monostatic sensor (i.e. where the scattered radiation
 86 is received at approximately the same position from which it was transmitted), \underline{k} is three
 87 dimensional complex (i.e. $\underline{k} \in \mathbb{C}^3$). Finally, it is possible to define the scattering mechanism
 88 as a normalized vector $\underline{\omega} = \underline{k}/|\underline{k}|$.

89 However, for most target detection applications the target observed by a SAR system is not
 90 a single idealized scattering target, but a combination of different targets which we refer to
 91 as a *partial target* [29], [34], [35]. In the context of ship detection, the sea is sometimes
 92 describable in terms of a single target (i.e. low entropy), however, especially when the
 93 backscattering is very low and when the sea is rough the determinism of its behavior could
 94 be removed. In order to characterize a partial target the second order statistics have to be
 95 considered

$$[C] = \langle \underline{k} \underline{k}^{*T} \rangle, \quad (3)$$

96 where $\langle \cdot \rangle$ is the finite averaging operator and $*$ is for complex conjugate. The Ψ_2 basis set
 97 most commonly used is the Pauli (i.e. $\underline{k} = [S_{HH} + S_{VV}, S_{HH} - S_{VV}, 2S_{HV}]^T$) since each
 98 of the components is sensitive to a specific type of single target [29]. Specifically, ideally
 99 $S_{HH} + S_{VV}$ represents a process that underwent an odd number of reflections (e.g. a single
 100 reflecting surface or a trihedral corner reflector), $S_{HH} - S_{VV}$ is an even bounce from a
 101 dihedral with a horizontal corner and S_{HV} is a dihedral with a corner oriented at 45 degrees
 102 with respect to the propagation plane (where 0 degrees stands for horizontal). In a maritime

103 context, it is expected that the $S_{HH} + S_{VV}$ image will be more dominant over the sea surface,
 104 while the ship would have a strong component in $S_{HH} - S_{VV}$ or S_{HV} (depending on ship
 105 orientation). The covariance matrix expressed with the Pauli basis is often referred to as
 106 Coherency matrix, $[T]$.

107 *B. Entropy detector*

108 The Polarimetric Entropy can be calculated exploiting the Cloude-Pottier decomposition
 109 [32]. The latter is based on the diagonalization of the covariance or coherency matrix (as de-
 110 fined in eq. 3). $[C]$ is an Hermitian semi-positive definite matrix. Therefore it can always be
 111 diagonalized. The eigenvalues are real positive and the eigenvectors form an ortho-normal
 112 basis for the space of the scattering vectors (a basis for which the three decomposed compo-
 113 nents are uncorrelated) [29]. The eigenvalues can be arranged to evaluate the entropy, which
 114 quantifies the possible dominance of one scattering mechanism over the others. The entropy
 115 is defined as:

$$H = - \sum_{i=1}^3 P_i \log_3(P_i) \quad (4)$$

116 P_i are the probabilities of each eigenvalue and can be calculated as:

$$P_i = \frac{\lambda_i}{\lambda_1 + \lambda_2 + \lambda_3} \quad \forall i = 1, 2, 3 \quad (5)$$

117 where, λ_i are the eigenvalues.

118 As mentioned in the previous section, the entropy (or more generally other measures of
 119 depolarization) was proposed for ship detection [23]. The rationale behind this choice is
 120 that the sea has a rather deterministic polarimetric behavior that leads the pixels inside the
 121 averaging window to be rather coherent to each other. This returns a low value for H . On
 122 the other hand, the ships are targets presenting large heterogeneity among pixels composing

123 the Region of Interest (ROI). Therefore averaging them together will result in confused po-
124 larimetric information (i.e. large entropy). The detector is simply finalized with a threshold
125 on H : $H > T_H$. In the following the value used for the threshold is 0.5, since this showed to
126 provide the best detection performances. An automatic algorithm could be exploited, setting
127 the threshold fitting some statistical distribution of the sea clutter. In this comparison, the
128 supervised approach is preferred since it assures that the threshold is selected optimally (i.e.
129 not introducing errors due to a wrong estimation of the statistical distribution).

130 C. CFAR with K -distributed intensity of S_{HV}

131 This detector exploits single polarization data and considers a Constant False Alarm Rate
132 (CFAR) based on a K -distribution for the image intensity [6]. In this context the S_{HV} polar-
133 ization (i.e. cross polarization) channel was found to provide the best contrast between ships
134 and sea clutter for the incidence angle considered in this study (around 24 degrees) [6]. The
135 K -distribution is considered here because it was proved to model with adequate accuracy the
136 statistical behavior of texture for the sea clutter [6]. The selection of the threshold follows
137 a CFAR methodology where the probability of false alarm can be selected depending on the
138 specific applications. In this work, the value for the Probability of False Alarm (P_f) was
139 selected as 10^{-5} and the integrals were solved numerically. The algorithm exploited here
140 did not use local windows and the threshold was set selecting an area of 20 x 100 sea pixels
141 for each sector of 1000x5000 SLC pixels. This is to reduce the computational time of the
142 algorithm [6].

143

III. POLARIMETRIC NOTCH FILTER

144 A. Mathematical Derivation

145 The ship detector presented in this paper shares the same general methodology of the
 146 Geometrical Perturbation - Partial Target Detector (GP-PTD). More details regarding the
 147 mathematical and physical justification of the algorithm can be found in [36], [37], [38], [4].

The first step is to construct a vector containing the second order statistics of the observed target. A feature partial scattering vector is introduced:

$$\begin{aligned} \underline{t} = \text{Trace}([C]\Psi_3) &= [t_1, t_2, t_3, t_4, t_5, t_6]^T = \\ &= [\langle |k_1|^2 \rangle, \langle |k_2|^2 \rangle, \langle |k_3|^2 \rangle, \langle k_1^{*T} k_2 \rangle, \langle k_1^{*T} k_3 \rangle, \langle k_2^{*T} k_3 \rangle]^T, \end{aligned} \quad (6)$$

148 where Ψ_3 is a complete set of 6x6 basis matrices under a Hermitian inner product. \underline{t} lies
 149 in a subspace of \mathbb{C}^6 representing all the physically feasible partial targets. The normalized
 150 version of \underline{t} can be considered: $\hat{\underline{t}} = \underline{t}/\|\underline{t}\|$. After a series of mathematical manipulations, the
 151 final expression of the PTD is:

$$\gamma_d = \frac{1}{\sqrt{1 + \text{RedR} \left(\frac{\underline{t}^{*T} \underline{t}}{|\underline{t}^{*T} \hat{\underline{t}}_T|^2} - 1 \right)}} > T_n. \quad (7)$$

152 where $\hat{\underline{t}}_T$ represents the signature of the target to be detected (and can be any unitary vector
 153 in the space of the physically feasible targets), \underline{t} is the partial vector extracted from the scene
 154 (i.e. observables), T_n is the threshold and RedR is a detector parameter that can be set using
 155 a rationale based on the SCR [37].

156 The idea behind the GP-PNF is to build an algorithm that is able to identify any partial
 157 target which is different from the background clutter. In the case of ship detection, the

158 background is the sea. A conventional model for the electromagnetic scattering from the
 159 ocean's surface is the Bragg scattering model [29], [39]. Details on the Bragg model are
 160 not presented in this paper since the GP-PNF does not make any assumption regarding the
 161 specific behavior of the sea, as long as its backscattering is locally homogeneous.

162 Following the new vector formalism, the sea clutter can be completely characterized with
 163 a vector in a six dimensional complex space, \underline{t}_{sea} . On the other hand, the targets of interest
 164 can have a large variety of polarimetric signatures depending on orientation, material and
 165 structure of the vessel and a single vector would not be sufficient to identify any possible ship.
 166 The GP-PNF approach is to say that anything looking different from the sea background is
 167 a valuable target. In other words, this is equivalent to saying that the targets of interest lie
 168 in the complement orthogonal subset of the sea vector (five dimensional complex subset).
 169 Please note, in its formulation the proposed algorithm is quite general and can be used for
 170 detection of any target that is polarimetrically different from the background (even for land
 171 application, as long as the background has a stable polarimetric response). In case of sea
 172 observation, targets different from the sea would be ships, but also buoys, icebergs, wind
 173 turbines, small islands, etc.

174 Details regarding the mathematical derivation of the GP-PNF can be found in [1], [2], [3],
 175 [4], here only the final detector expression is presented for sake of brevity:

$$\gamma_n = \frac{1}{\sqrt{1 + \frac{RedR}{\underline{t}^{*T}\underline{t} - |\underline{t}^{*T}\hat{\underline{t}}_{sea}|^2}}} > T_n. \quad (8)$$

176 B. Dual-Polarimetric GP-PNF

177 Dual-polarimetric data are generally not sufficient to completely describe a partial target,
 178 however, in some instances the coherent acquisition of four polarizations is not feasible and

179 only two coherent acquisitions can be performed. The latter acquisition scheme generally
 180 takes name of dual-polarimetric mode [20], [29].

181 A dual-polarimetric scattering vector can be introduced as $\underline{k}_d = [k_1, k_2]^T$, with k_1 and
 182 k_2 being complex numbers (for instance S_{HH} and S_{VV}). The covariance matrix can be
 183 estimated as:

$$[C_d] = \begin{bmatrix} \langle |k_1|^2 \rangle & \langle k_1^{*T} k_2 \rangle \\ \langle k_2^{*T} k_1 \rangle & \langle |k_2|^2 \rangle \end{bmatrix}. \quad (9)$$

184 Subsequently, a three dimensional partial feature vector can be built: $\underline{t}_d = Trace([C_d]\Psi_2) =$
 185 $[\langle |k_1|^2 \rangle, \langle |k_2|^2 \rangle, \langle k_1^{*T} k_2 \rangle]^T$. Finally, the dual-polarimetric detector is:

$$\gamma_{dn} = \frac{1}{\sqrt{1 + RedR \frac{1}{\underline{t}_d^{*T} \underline{t}_d - |\underline{t}_d^{*T} \hat{\underline{t}}_{dsea}|^2}}} > T_n, \quad (10)$$

186 where $\hat{\underline{t}}_{dsea}$ is the normalized dual-polarimetric signature of the sea.

187 The mathematical derivations are presented in more details in [2], [3], [40].

188 C. Parameter Selection

189 The GP-PNF has two parameters: T_n and $RedR$, which will determine the sensitivity of
 190 the detector. This means that one can be arbitrarily selected in its entire range of values (e.g.
 191 $T_n \in]0, 1[$ and $RedR \in]0, \infty[$) and the other is set based on the level of sensitivity required
 192 by the detector. The solution followed in this paper is to set the threshold to $T_n = 0.9$ and
 193 choose the $RedR$ based on the minimum intensity P_T^{min} of a target of interest in the subset
 194 complementary to the vector representing the sea:

$$RedR = (P_T^{min})^2 \left(\frac{1}{T_n^2} - 1 \right). \quad (11)$$

195 The square on P_T^{min} comes from the product $\underline{t}^{*T}\underline{t}$ which squares each of the components of
 196 the covariance matrix.

197 The selection of a minimum target is needed to take into account some small heterogene-
 198 ity in the sea and statistical errors in the estimations (due to finite number of samples). The
 199 choice of the P_T^{min} depends on the vessel that the users are interested to detect. In case
 200 that these are supposed to have large scattering (e.g. they are more than a hundred meters
 201 long or they contain large metallic structures) a larger value will reject all the impurities in
 202 the data, while if the vessels are expected to do not backscatter much (e.g. they are around
 203 10 meters long or made of low reflecting materials) a smaller P_T^{min} should be chosen, but
 204 some problems may arise with artifacts and ambiguities. This image defects are generated
 205 by processing errors and may be interpreted as ships, since they appear as bright points in
 206 the image [41]. Therefore, in such cases a good pre-processing (or post-processing) step for
 207 cleaning ambiguities should be done besides the GP-PNF. In the dataset available, it is pos-
 208 sible to observe only one strong azimuth ambiguity (as illustrated in the section concerning
 209 false alarms analysis).

210 In this paper, the value chosen for the P_T^{min} is $-15dB$ that corresponds to 0.029 in linear
 211 scale. This value was chosen analyzing the curves of false alarms in Section V (the reader
 212 is redirected to this section for further details). The choice of $P_T^{min} = -15dB$ leads to
 213 $RedR = 2 \cdot 10^{-4}$. As a final remark it has to be said that the choice of P_T^{min} will be
 214 clearly dependent on the specific sensor exploited and the typology of targets under analysis.
 215 Parameters that can strongly influence the selection of P_T^{min} are frequency, resolution, noise
 216 floor, dimension and material of vessels. The weather conditions clearly impact the detection
 217 performance, however, as showed in [40] the GP-PNF is theoretically relatively stable against
 218 weather conditions as long as the sea keeps on behaving as a locally homogeneous clutter.

219 Further work should be carried out to understand if sea clutter is locally homogeneous also
220 with particularly high sea states (this may also be function of the sensor resolution). In
221 other works of the authors, TerraSAR-X and RADARSAT-2 data were considered and the
222 values for P_T^{min} that were found to provide good results were respectively $-7dB$ and $-25dB$.
223 Currently, work is ongoing on devising an algorithm able to set the threshold automatically
224 for any detection tasks (any frequency and resolution). In this context, some statistical test
225 may reveal promising, however, the derivation of the theoretical Probability Density Function
226 (pdf) of the GP-PNF output is not trivial and the test with some well-known distributions
227 may reveal very coarse. Additionally, some methodologies may consider iterative global
228 optimizations.

229 Regarding the selection of the filter null \hat{t}_{sea} , this is performed locally with a large mov-
230 ing window W_{tr} . Then the detection is performed within a smaller target window W (more
231 details about window sizes are provided in the validation section). A simple solution with
232 moving boxcar averaging (without guards) makes the detector particularly fast (1500x4000
233 pixels processed in few seconds with a regular desktop computer), and therefore feasible for
234 real time applications. Moreover, the use of guards was tested and it did not show significant
235 improvements. The reason of this is that the detection is performed on the base of the polari-
236 metric signature and not the intensity of the signal. Therefore, a contamination of W_{tr} will
237 not make the sea signature equal to the one of the target inside W , but just a combination of
238 of the different signatures of the extended vessel (if this is imaged in more than one pixel)
239 and the sea clutter [40].

240

IV. VALIDATION WITH ALOS-PALSAR DATA

241 *A. Presentation of the datasets*

242 The current GP-PNF validation experiment is performed with ALOS-PALSAR data. The
243 algorithm was previously tested with different frequencies as C-band (RADARSAT-2) [2]
244 and X-band (TerraSAR-X) [1]. This is the first time ever that the GP-PNF is tested with
245 L-band data and it is interesting to understand if for this frequency polarimetry adds a contri-
246 bution to enhance ship detection performance. L-band may represent an interesting scenario
247 since the sea backscattering is expected to be relatively low at this frequency [39]. The
248 dataset covers the Tokyo Bay area (Japan), which is renowned to have a large traffic of ves-
249 sels. The acquisition was performed on the 9th of October 2008, (10:19 am local time).
250 In this analysis Single Look Complex (SLC) data were considered. In order to reduce the
251 speckle variation, a filtering was performed by the GP-PNF itself as described in the fol-
252 lowing. The resolution in ground range is 27 m, while in azimuth is 4.9 m. More details
253 regarding the images are the following: the slant range resolution is 11.1 m, while the pixel
254 spacing in slant range is 9.4 m (please note SAR images are over-sampled, therefore pixel
255 spacing and resolution may be different); the pixel spacing in azimuth is 3.6 m. The inci-
256 dence angle of these acquisitions is approximately 24 degrees.

257 The algorithm initially multi-looks the data 1x5 (range x azimuth) to make the pixel more
258 squared on the ground. Subsequently, a target moving window of 5x5 pixels is exploited for
259 the detection. Clearly, the samples are not all independent of each other and an Equivalent
260 Number of Looks (ENL) can be calculated. In the following experiments, this is $ENL = 50$.
261 In order to get a good estimation of the targets in the scene, as a general recommendation,
262 the ENL should be kept higher than 25. Clearly, in case that the detection is focused on

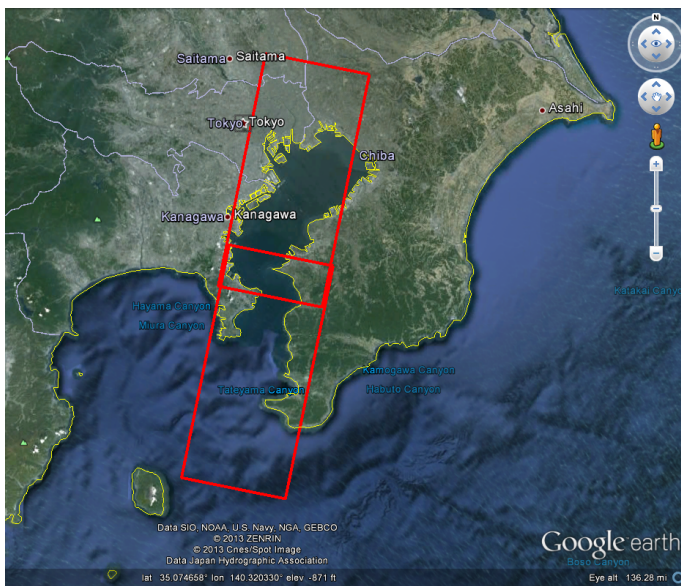
263 very small vessels, fewer pixels could be used. The big averaging window W_{tr} exploited to
264 extract the value of \hat{t}_{sea} is 20x20 pixels (after the initial multi-look) ending up with more
265 than 800 ENL.

266 During the acquisition a ground survey was carried out combining different instruments.
267 A video of vessels crossing a portion of the Bay was captured in cooperation with a X-band
268 ground-based radar. Both the video camera and radar were located on the top of the National
269 Defense Academy building (the west shore of the bay) at an altitude of approximately 100m
270 over the sea level [42]. Finally, Automatic Identification System (AIS) data were acquired,
271 but unfortunately only six vessels had an operating AIS transponder. Combining all this
272 information, the location of vessels was reconstructed.

273 Regarding the sea state, the significant waveheight is 0.7m (three in Beaufort Scale) in
274 the direction 190° from North. The period is 1.8sec and the wind speed is 11.2m/s (strong
275 breeze: six in Beaufort Scale) in the direction 20° .

276 In order to have an idea of the geographical location of the test area, the aerial photo-
277 graph (taken from Google Earth) of Tokyo bay is presented in Figure 1, where the rectangles
278 represent the ALOS-PALSAR acquisition.

279 Before proceeding with the detection, it is interesting to have a preliminary look at the
280 polarimetric information visualizing the Pauli RGB composite image for the scene (Figure
281 1.b). Again, the RGB images are pre-processed multi-looking 1x5 the coherency matrix.
282 The Pauli basis is particularly valuable for the physical interpretation that can be attached to
283 its components. Specifically, the blue is sensitive to surface scattering, in this case the sea.
284 Looking at the image it is also clear the basic idea of the GP-PNF, since the sea background
285 appears polarimetrically homogeneous (i.e. it is blue everywhere except for spots of low
286 backscattering). Several targets are visible in the RGB image. The dataset is particularly



(a) Google Earth aerial photograph



(b) Pauli RGB

Fig. 1. ALOS-PALSAR quad-polarimetric dataset on Tokyo Bay (35.294451° , 139.785816°), 9^{th} of October 2008: (a) Google Earth aerial photograph with a rectangle indicating the ALOS-PALSAR acquisition; (b) Pauli RGB of the entire dataset, image size: 30x68km. Data provided by JAXA.

287 valuable since the scattering from the sea appears to be particularly high, with maximum
288 values of the $S_{VV} \sigma^0$ that are proximal to 0.7 (-1.5dB). Besides the weather conditions, this
289 is due to the incidence angle that is relatively steep (24 degrees).

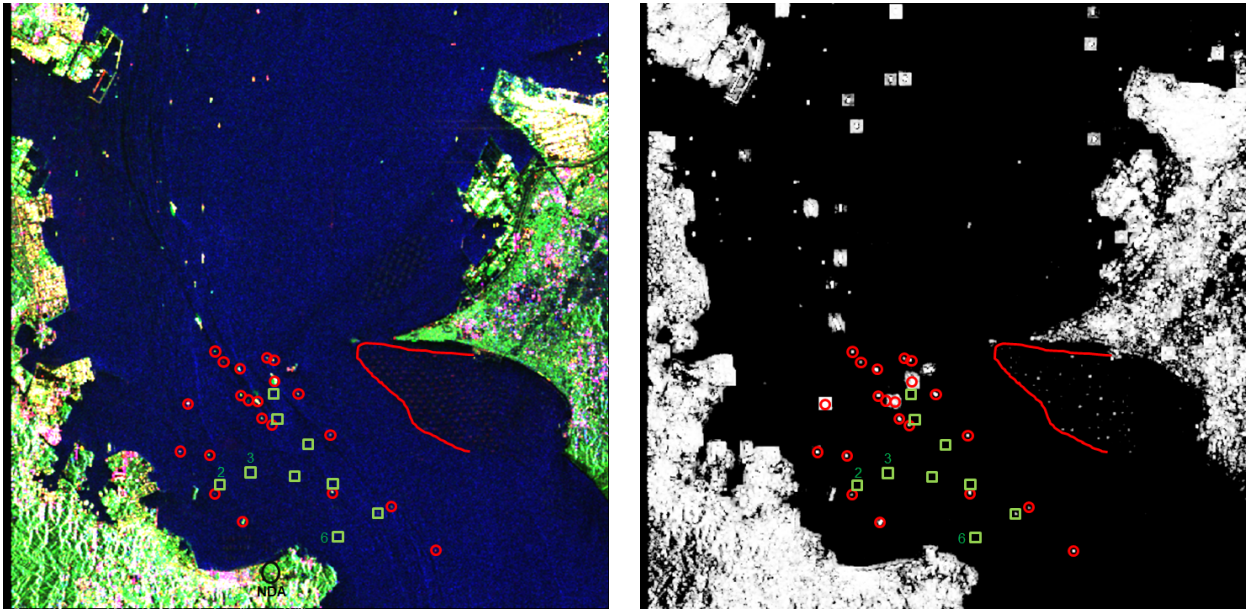
290 A.1 Detection over image crops: ground survey area

291 The RGB of the area of interest is presented in Figure 2.a with markers to identify features
292 of interest. The red circles indicate vessels that were visible in the ground survey and can
293 be identified in the RGB image. Green rectangles are vessels visible in the camera images
294 but not in the RGB. This means that a visual inspection of the SAR images was not allowing
295 detection. Some of the rectangles have a number indicating that this is not a single vessel
296 but a cluster of small vessels very close each other. The area surrounded by the red line
297 presents a seaweed farm (please note, inspection of Google Earth images showed that there
298 is also another small seaweed farm more in the north and one close to NDA). In the following
299 analysis, the same symbols are kept in order to compare the detection results with the visual
300 inspection.

301 The GP-PNF detection mask with quad-pol is showed in Figure 2.b.

302 As it can be observed all the vessels in the red circles are detected by the GP-PNF quad-
303 polarimetric detector. Additionally, one of the vessels that is not visible in the RGB (green
304 rectangle) can now be detected, leading to 22 detected targets and 16 missing. If clusters of
305 vessels are counted as one (since several small vessels may be in the same target window),
306 the number of missing clusters would be 8. From the detection mask it is not possible to
307 identify any false alarm. Finally, many of the seaweed platforms are identified, showing
308 detection capabilities also for these wooden targets with low backscattering.

309 A comparison with dual-pol HH/VV and HH/HV is provided in Figure 3. An accurate



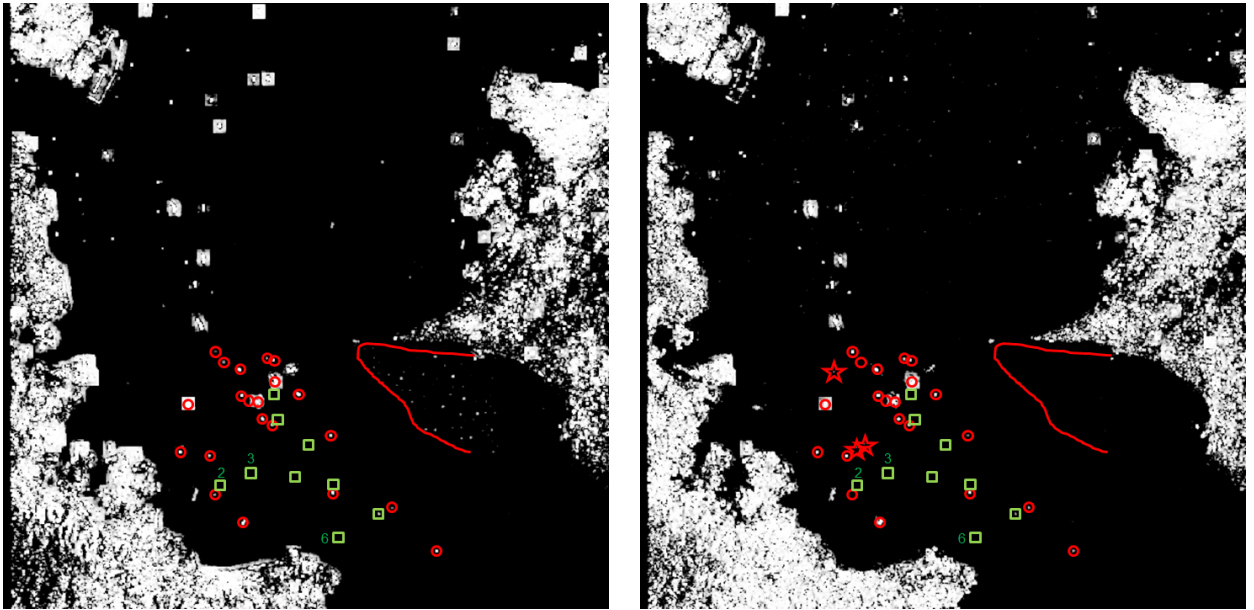
(a) RGB Pauli

(b) Quad-pol GP-PNF

Fig. 2. GP-PNF over the area provided of video survey (ALOS-PALSAR, JAXA): (a) RGB Pauli (b) Quad-pol GP-PNF with labels ($P_T^{min} = -15dB$). Image size: 23x18km. (35.293664° , 139.791927°)

310 inspection of the detection masks shows that the HH/VV mode is identifying the same targets
 311 as for the quad-pol (22 vessels). The HH/VV detector used exactly the same parameters
 312 as the quad-polarimetric version. On the other hand, the HH/HV performance is slightly
 313 degraded with 20 vessels detected. In order to improve the detection capabilities of the
 314 HH/HV version the value of the P_T^{min} had to be lowered to 0.01 or -20dB. If the same value
 315 of the quad-pol version was used, only 14 vessels would be detected. Unfortunately, reducing
 316 the value of P_T^{min} may increase the false alarms as it can be observed in this test were three
 317 false alarms are visible (red stars). They appear as isolated points, therefore a morphological
 318 filter may be used to remove them. The authors leave this as future work.

319 The final test is performed comparing the GP-PNF with the entropy detector and the K-
 320 distributed CFAR over the S_{HV} intensity (Figure 4). The entropy detector is able to identify
 321 21 vessels (one less than the GP-PNF). Specifically, the algorithm appears particularly suited



(a) HH/VV GP-PNF

(b) HH/HV GP-PNF

Fig. 3. GP-PNF over the area provided of video survey (ALOS-PALSAR, JAXA): (a) Dual-pol HH/VV GP-PNF ($P_T^{min} = -15dB$); (b) Dual-pol HH/HV GP-PNF ($P_T^{min} = -20dB$). Image size: 23x18km. ($35.293664^\circ, 139.791927^\circ$)

322 to identify the seaweed areas where almost all the platforms are detected [43]. Additionally,
 323 also the other two farms are partially detected. Please note, a similar result for seaweed farms
 324 detection is repeatable employing the quad-pol GP-PNF if the value of P_T^{min} is divided by
 325 two or reduced of 3dB (i.e. $P_T^{min} = -18dB$), but this introduces also two false alarms (the
 326 detection mask is not showed for sake of brevity). Unfortunately, the entropy suffers from
 327 false alarms, occurring when the backscattering level of the sea is low (some of these points
 328 are indicated in the images with stars, but more than 20 isolated points could be counted).
 329 This is because low backscattering leads to a scattering largely affected by noise that confuses
 330 the polarimetric behavior increasing the entropy. Finally, this is supposed to be one of the
 331 reasons (but not the only one) that contributes to the detection of the seaweed (laver) farms,
 332 since these structures dampen the waves lowering the backscattering.

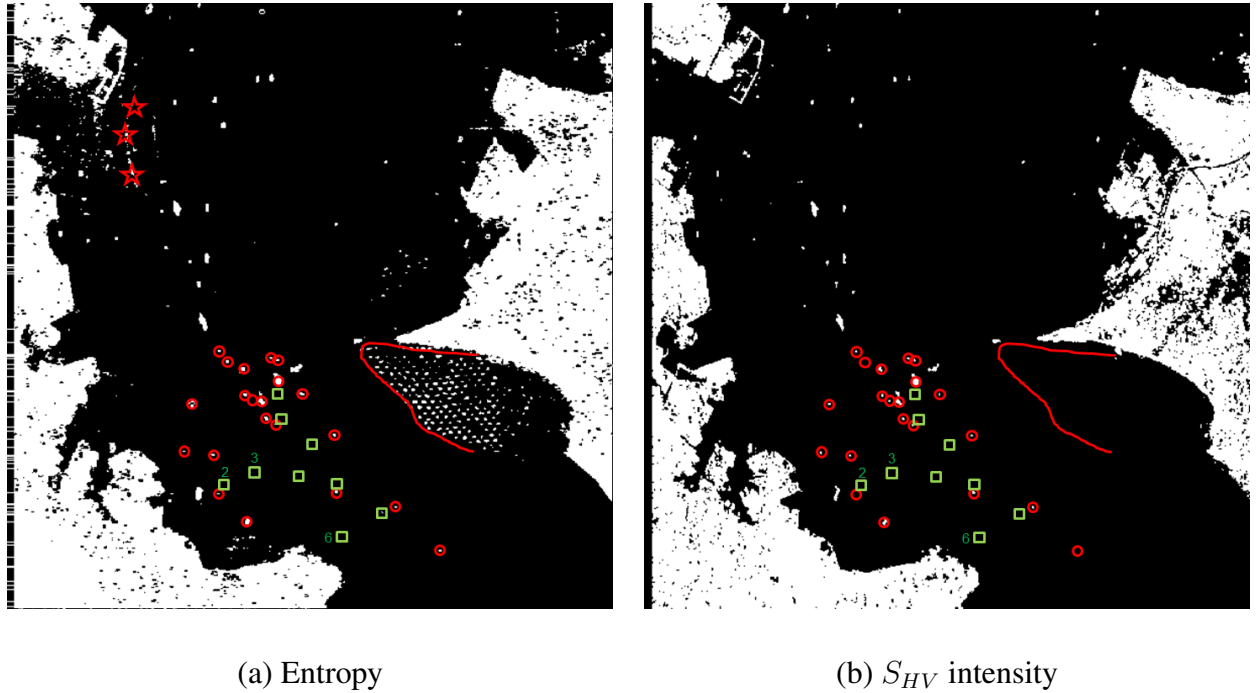


Fig. 4. Comparison with the entropy detector and the K-distributed S_{HV} intensity for the area with ground survey: (ALOS-PALSAR, JAXA): (a) Entropy with threshold 0.5 (b) CFAR with $P_f = 10^{-5}$. Image size: 23x18km. (35.293664° , 139.791927°)

333 The CFAR with the S_{HV} polarization presents a detection mask with lower performance.
 334 Only 18 vessels are detected (four less than the quad-pol GP-PNF). Moreover, all the sea-
 335 weed platforms are missing in the detection.

336 To summarize the results, Table I presents the number of vessels detected, missed and false
 337 alarms for the area provided of video survey. The best detection performance on vessels is
 338 showed by the GP-PNF quad-pol and HH/VV mode, with 22 over 38 vessels detected and
 339 no false alarms. For the seaweed areas, the entropy appears to outperform the other algo-
 340 rithms [43], but care has to be taken when using the entropy, since false alarms may occur
 341 when the signal is low and seaweed farms are characterized by low backscattering (therefore
 342 a pre-filtering of dark pixels would exclude the seaweed farms). The worst detection perfor-
 343 mance is returned by the S_{HV} K-distributed CFAR. This is because the information of the

TABLE I

SUMMARY OF DETECTION RESULTS OVER THE VIDEO SURVEYED AREA AS PRESENTED IN THE

DETECTION MASKS			
Detector	Detections	Missing	False Alarms
GP-PNF (Quad-pol)	22	16(8)	0
GP-PNF (Dual HH/VV)	22	16(8)	0
GP-PNF (Dual HH/HV)	20	18(9)	3
CFAR (S_{HV})	18	20(11)	0
Entropy	21	17(9)	> 20

344 co-polarizations is lost and they are particularly valuable to characterize the sea backscatter-
 345 ing.

346 Regarding the missing vessels we believe that higher resolution data may be beneficial
 347 to detect them. These vessels are not visible at all in the RGB image (not even after large
 348 zooming and inspecting the SLC of each polarimetric channel). They are supposed to be
 349 made of fiber-glass (without extensive metallic structures) and from the video survey they
 350 look particularly small (around or smaller than 10m).

351 A.2 Detection over image crops: Tokyo Bay Aqua Line

352 The second image crop includes the Tokyo Bay Aqua Line (visible as a straight line on
 353 the East Coast). The RGB and quad-pol detection masks are presented in Figure 6 with
 354 some markers identifying features of interest. As for the previous case the backscattering
 355 from the sea is quite high (i.e. $\sigma_{VV}^0 \approx -1.5dB$). The GP-PNF detects the points that
 356 could be easily attributed to vessels after a visual inspection of the RGB image. Please note,

357 the effect of enlarging the detection points is a consequence of the training window W_{tr} .
358 When a bright target is analyzed the detection starts from the moment when the target enters
359 the moving window W_{tr} . It is important to remark that this second area is not covered by
360 ground survey, therefore only qualitative results can be provided. Nevertheless, the test is
361 interesting to evaluate the stability of the choice for detector parameters and to compare
362 different polarimetric modes.

363 The red ellipses identify areas where a line of targets is detected, however, looking at the
364 RGB image no targets are visible there. In order to check for possible presence of targets,
365 a Google Earth image of the area is provided in Figure 5. These detected points correspond
366 to a mix of wooden water barrier approximately 20 m wide and 50 m long (i.e. flower
367 shaped structures) and laver farms (i.e. dark stripes). In the SAR image they have a very
368 weak backscattering which makes them impossible to detect using intensity, however the
369 polarimetric information allows their separation from the sea background. A test of the
370 quad-pol GP-PNF was performed using $P_T^{min} = -18dB$ and not presented here for sake
371 of brevity. The mask shows that with the lower threshold more targets are detectable, but
372 since some of them are very weak in the RGB image it was not possible to state with some
373 objectivity that they represent vessels.

374 The red triangle delineates an area that is suspected to be affected by image artifacts,
375 specifically azimuth ambiguities from the nearby coast. Unfortunately, ground measure-
376 ments are not provided to understand if this is an artifact or not. However, it is also impor-
377 tant to notice that such artifacts are not distinguishable from genuine vessels and therefore
378 they are detected by the algorithms. Fortunately, some pre-processing could be exploited to
379 remove them before to run the detector.

380 The dual-pol modes HH/VV and HH/HV are presented in Figure 7. The two circles on

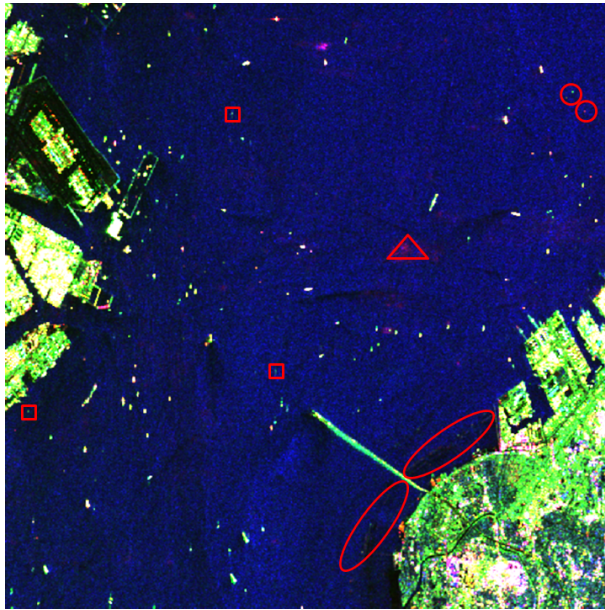


Fig. 5. Google Earth aerial photograph of some of the detected targets just beside Tokyo Bay Aqua Line.

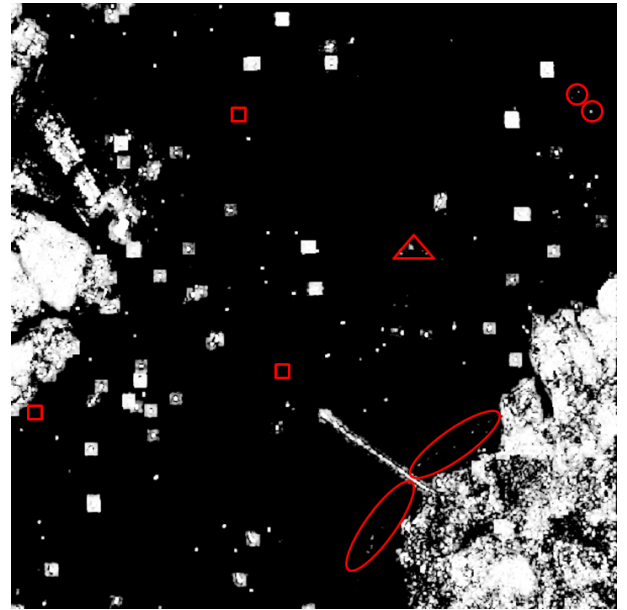
381 the up right corner present an interesting phenomenon: each of the dual-pol detectors can
 382 identify only one of the vessels, while the quad-pol detects both. Dual-polarimetry only
 383 considers partial information and when a target has no projection on the subspace observable
 384 by the two acquired channels then it will be missed in the detection mask.

385 The red diamonds indicate missing targets. It appears that the performance of HH/VV
 386 is still very close to the quad-pol mode, only for few exceptions (as the vessel in the red
 387 circle). HH/HV has several targets missing, among others, the small water barriers. Finally
 388 the red rectangles indicate points detected exclusively by the HH/HV mode. Looking at
 389 the RGB Pauli they appear as possible vessels, but of course they may just be false alarms.
 390 This is possible because the threshold used for the HH/HV is lower and therefore it allows
 391 the identification of vessels with a lower P_T^{min} . Interestingly, the quad-pol GP-PNF can
 392 detect these points if the threshold P_T^{min} is divided by two (i.e. $P_T^{min} = -18dB$), but this
 393 introduces at least two apparent false alarms. For the HH/VV mode, reducing the value of
 394 P_T^{min} to $-18dB$ allows only the detection of one of these three points.

395 The last test is with the other two detectors (Figure 8). As for the previous case, the
 396 entropy has good detection performance, especially for the small wooden barriers close to

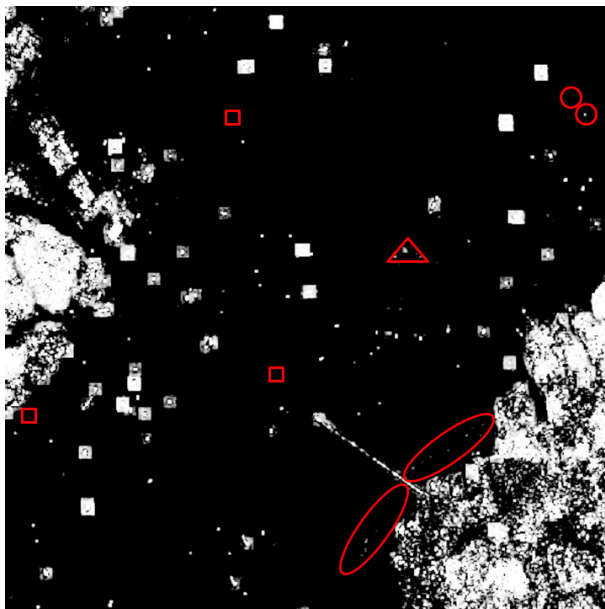


(a) Pauli RGB

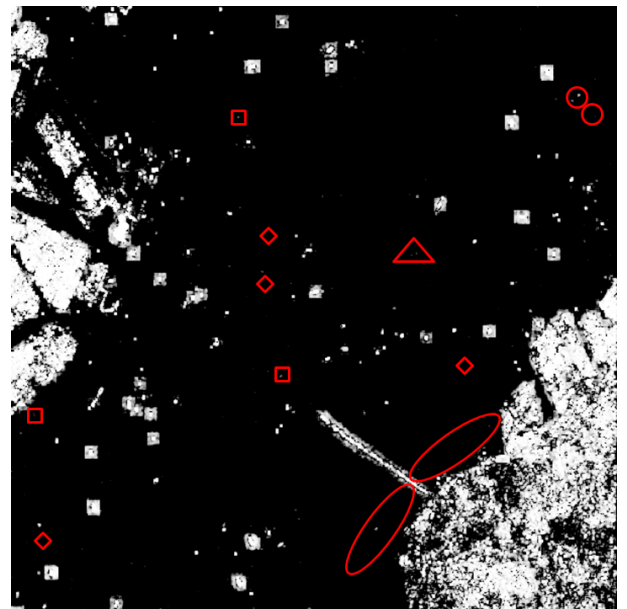


(b) Quad-pol GP-PNF

Fig. 6. GP-PNF over the area with Tokyo Bay Aqua Line (ALOS-PALSAR, JAXA): (a) RGB Pauli (b) Quad-pol GP-PNF ($P_T^{min} = -15dB$). Image size: 23x18km. ($35.520243^\circ, 139.850018^\circ$)



(a) HH/VV



(b) HH/HV

Fig. 7. GP-PNF over the area with Tokyo Bay Aqua Line (ALOS-PALSAR, JAXA): (a) Dual-pol HH/VV GP-PNF ($P_T^{min} = -15dB$); (b) Dual-pol HH/HV GP-PNF ($P_T^{min} = -20dB$). Image size: 23x18km. ($35.520243^\circ, 139.850018^\circ$)

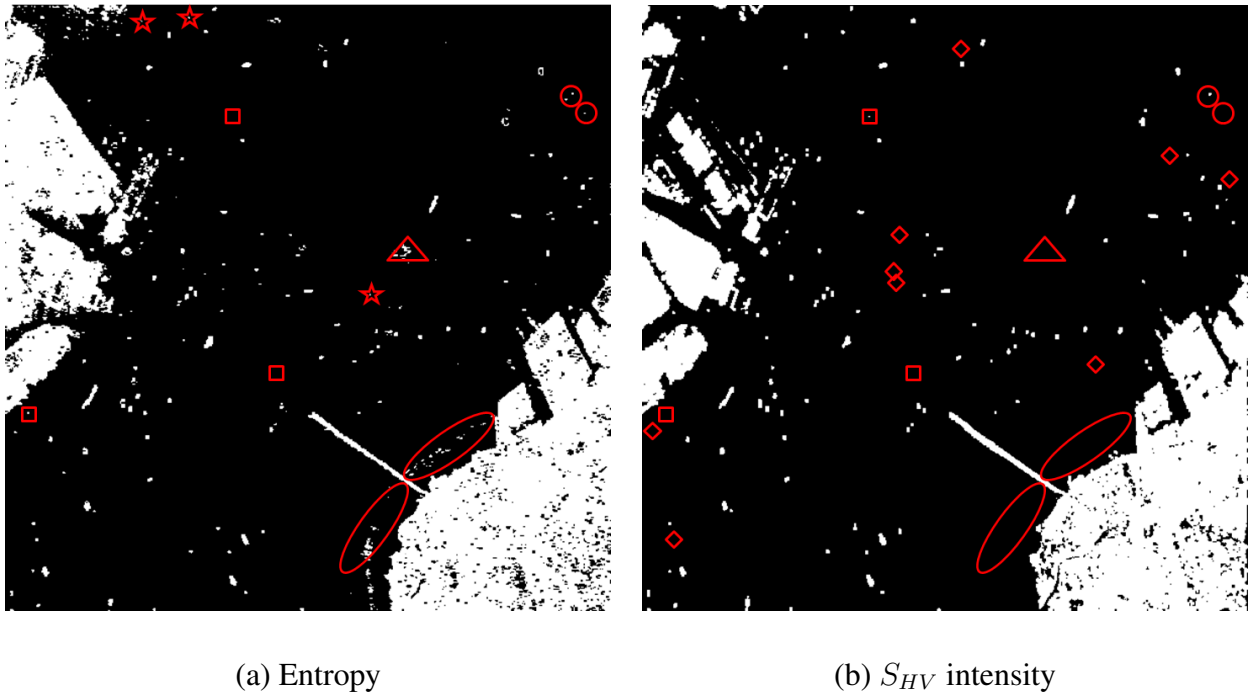


Fig. 8. Comparison with the entropy detector and the k distributed S_{HV} intensity for the area with ground survey: (ALOS-PALSAR, JAXA): (a) Entropy with threshold 0.5 (b) CFAR with $P_f = 10^{-5}$. Image size: 23x18km. (35.520243° , 139.850018°)

397 the Aqua Line. It is also possible to detect one of the targets in the red rectangles (the same
 398 detected by HH/VV with $P_T^{min} = -18dB$). Unfortunately, the algorithm is again affected
 399 by false alarms where the backscattering is low (some of the points are indicated with red
 400 stars). The S_{HV} intensity detector is able to detect many targets that can be interpreted as
 401 vessels, but several are missing (indicated by nine red diamonds). The intensity detector is
 402 also able to identify one of the targets in the red rectangles.

403 V. FALSE ALARMS AND ROC CURVES

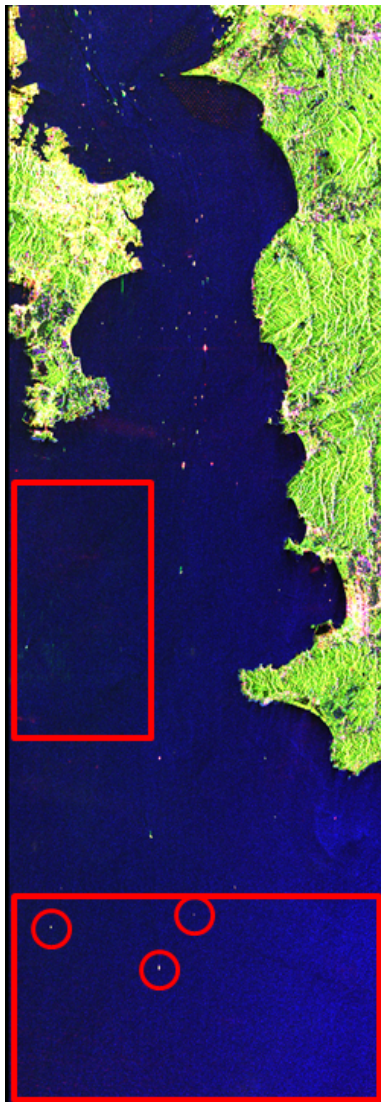
404 A. False alarms

405 This final section is focused on investigating more quantitatively the false alarm rate on
 406 another area of the ALOS dataset(Figure 9.a). This water region is outside the entrance

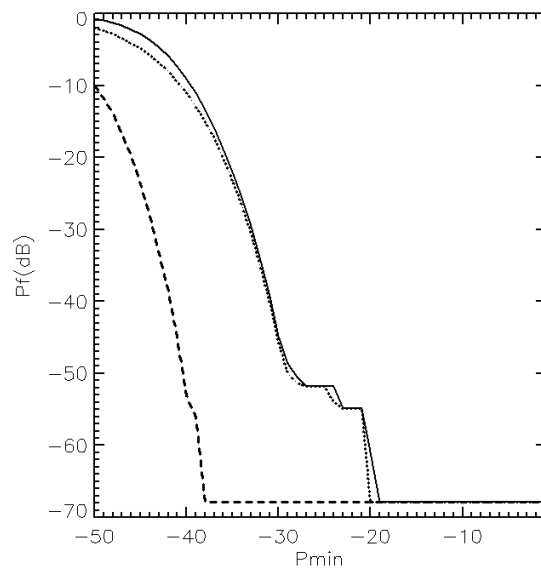
407 of Tokyo Bay and therefore expected to have less presence of vessels (however a proper
 408 ground survey is not available). In the RGB Pauli, the two rectangles indicate the areas
 409 used to extract the statistics for false alarms (i.e. absence of targets). In the rectangle at the
 410 bottom of the image, three vessels are evident (zooming in, their wakes can be observed).
 411 In the following analysis, the pixels corresponding to these three vessels are removed. The
 412 uppermost rectangle presents an area where some bright pixels are visible. Zooming in
 413 the area, these pixels are distributed on a large area resembling an artifact (i.e. azimuth
 414 ambiguities). Nevertheless, we decided to include these pixels in order to provide a more
 415 general analysis.

416 In this experiment, the probability of false alarm is calculated as the number of detected
 417 SLC pixels (before multi-look), over the total number of SLC pixels. Considering both
 418 the areas cover approximately 6.1 million pixels, the minimum P_f that can be estimated is
 419 equal to $1.64 \cdot 10^{-7}$. With the parameters exploited for the previous tests ($P_T^{min} = -15dB$),
 420 the quad-pol GP-PNF shows no false alarms in the entire areas. However, to have a more
 421 exhaustive test, it is possible to plot the P_f as a function of P_T^{min} (expressed in dB). The
 422 results are showed in Figure 9. The GP-PNF quad-pol and HH/VV dual-pol exhibit a similar
 423 behavior, where the quad-pol shows a slightly higher P_f . The detection capability of quad-
 424 pol is higher than HH/VV dual-pol, therefore lower P_T^{min} are needed to obtain detection (in
 425 other words, the quad-pol mode collects more power coming from the target, compared to
 426 dual-pol modes). detections start appearing before in the quad-pol detector when P_T^{min} is
 427 varied. The HH/HV shows a lower detection capability, which in this context translates in
 428 better rejecting of false alarms.

429 In order to keep the false alarm rate very small (i.e. none of the 6.1 million pixels de-
 430 tected), the P_T^{min} should not be smaller than $-20dB$ for quad-pol and HH/VV and $-37dB$



(a) Pauli RGB



(b) P_f varying P_T^{min}

Fig. 9. Analyzing the Probability of False Alarms: (a) Pauli RGB image of the area exploited (ALOS-PALSAR, JAXA); Red rectangles: areas used for the estimation of P_f ; Red circles: targets excluded by the analysis. Image size: 23x18km. (35.033164° , 139.741118°); (b) Plot of P_f varying P_T^{min} for the GP-PNF: Solid line: quad-pol; Dotted line: HH/VV dual-pol; Dashed line: HH/HV dual-pol.

431 for HH/HV. Please note, the minimum value of P_T^{min} can be lower than the noise floor, since
 432 P_T is the power corresponding to a target in the complementary space of the background
 433 clutter. As explained previously, thermal noise can be characterized with a unique \underline{t} vector
 434 and it is expected to be locally homogeneous, therefore it is possible theoretically to reject it
 435 with P_T^{min} much lower than the noise floor. False alarms are triggered as consequence of het-
 436 erogeneity or estimation error due to the finite number of samples (as showed in [40]). The
 437 latter fixes a boundary on the minimum value of P_T^{min} . As a final remark, it is important to
 438 keep in mind that these results depend largely on the specific dataset (e.g. different weather
 439 conditions or frequencies can lead to different plots).

440 B. ROC curves

441 B.1 Comparison of detectors

442 Once a meaningful analysis of P_f varying P_T^{min} is available this can be exploited in com-
 443 bination with an analysis of P_d (over the validated test area) to plot the Receiver Operating
 444 Characteristic (ROC) curve. The latter helps showing the detector performance indepen-
 445 dently of the specific threshold selected. These curves also allow a fair comparison between
 446 different detectors, since they are not based on the specific thresholds. In the previous sec-
 447 tion, detection masks for the HV intensity and the entropy were illustrated. In order to
 448 provide a larger validation another dual-pol detector is evaluated, which corresponds to set-
 449 ting a threshold on the intensity of the HH–VV polarimetric channel (i.e. it may be referred
 450 as a *dihedral* detector). The results are presented in Figure 10.a. The red lines are for the
 451 GP-PNF, while the black ones for the other detectors.

452 The ROC curves present a dual behavior for values of P_d below and above 0.85:

453 1. $P_d > 0.85$: Three detectors show good performance with results fairly close each other:

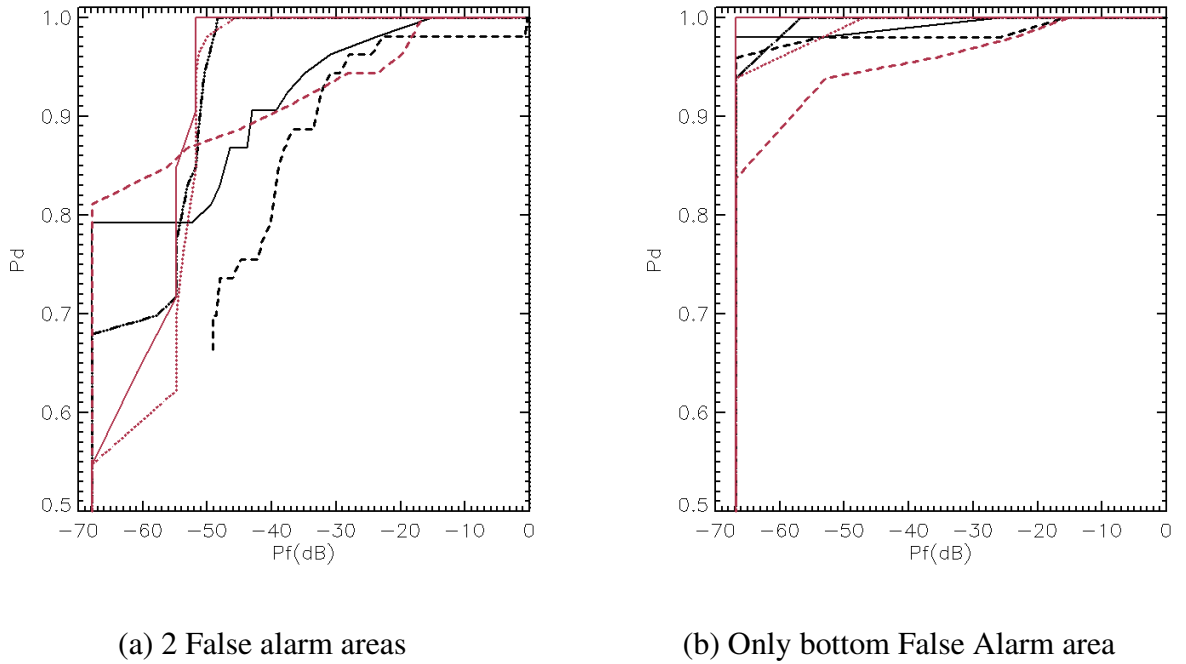


Fig. 10. ROC curves for GP-PNF (red) and other detectors (black). (a) Red solid line: quad-pol GP-PNF; Red dotted line: HH/VV GP-PNF; Red dashed line: HH/HV GP-PNF; Black solid line: HV intensity; Black dashed line: $HH - VV$ intensity; Black dash-dot line: entropy.

454 the quad-pol GP-PNF, the HH/VV GP-PNF and the entropy. The curves suggest that in this
 455 dataset it is possible to have $P_d \approx 1$ with P_f smaller than 10^{-5} .

456 2. $P_d < 0.85$: It appears that the ROC curves of the previous three detectors have a drastic
 457 drop for $P_f < 10^{-5}$, while the HH/HV GP-PNF and the HV intensity appear to be quite
 458 unaffected by this drop. The reason is most likely due to the presence of artifacts (probably
 459 azimuth ambiguities from the nearby Tokyo) in the uppermost area (upper red rectangle in
 460 Figure 9.a). In actual fact, these artifacts are visible in the RGB image and they appear to
 461 affect the co-polarizations channels more than the cross-polarization one. To prove these, the
 462 uppermost area was removed from the analysis and the ROC was calculated again exploiting
 463 only the bottommost area. The resulting ROC are showed in Figure 10.b. The order of the
 464 curves (i.e. ranking between detector) is quite unmodified (at exception of the HV intensity,

465 which gains some position) however the problem with the drop (artifacts) disappears.

466 To conclude, the ROC curves show that on this dataset the quad-pol GP-PNF provides the
 467 best performance among the tested detectors, although the results obtained by the dual-pol
 468 HH/VV GP-PNF and the entropy detector are fairly close. The ROC's suggest that if the
 469 dataset is free from artifacts, the quad-pol GP-PNF can provide a $P_f < 3 \cdot 10^{-7}$ with $P_d = 1$.
 470 However, in the more general case, where the dataset is expected to have some artifacts, the
 471 P_f should raise to 10^{-5} in order to keep $P_d = 1$.

472 A last remark should be made regarding the entropy detector. In this experiment, it shows
 473 good behavior with respect to false alarms, but in the previous tests (closer to the city) it was
 474 possible to observe many false alarms in correspondence of ship wakes (where the signal
 475 is particularly low). As mentioned previously, the entropy should not be applied when the
 476 backscattering is low and therefore the detection performance showed by the ROC is only
 477 valid where this assumption is fulfilled (i.e. the backscattering is relatively high).

478 B.2 Comparison of window dimensions

479 Finally, the ROC curves can be used to investigate the windows size that provides the
 480 best characteristic. Figure 11 shows the ROC when the target W and training windows W_{tr}
 481 are modified. The first plots consider a target window 5x5 (after the initial multi-looking),
 482 changing the dimension of the training window W_{tr} . While the second plots are for a target
 483 window 3x3. The solid lines are for $W_{tr} = 20$ (as the one exploited in the previous ex-
 484 periments), the dotted lines are for $W_{tr} = 30$ and the dashed lines are for $W_{tr} = 10$. The
 485 results are similar, however it can be noticed that if the background is not well characterized
 486 by a training window large enough, there may be a loss of detection performance. In these
 487 experiments, the combination that provides the best characteristics for $P_d = 1$ is a target

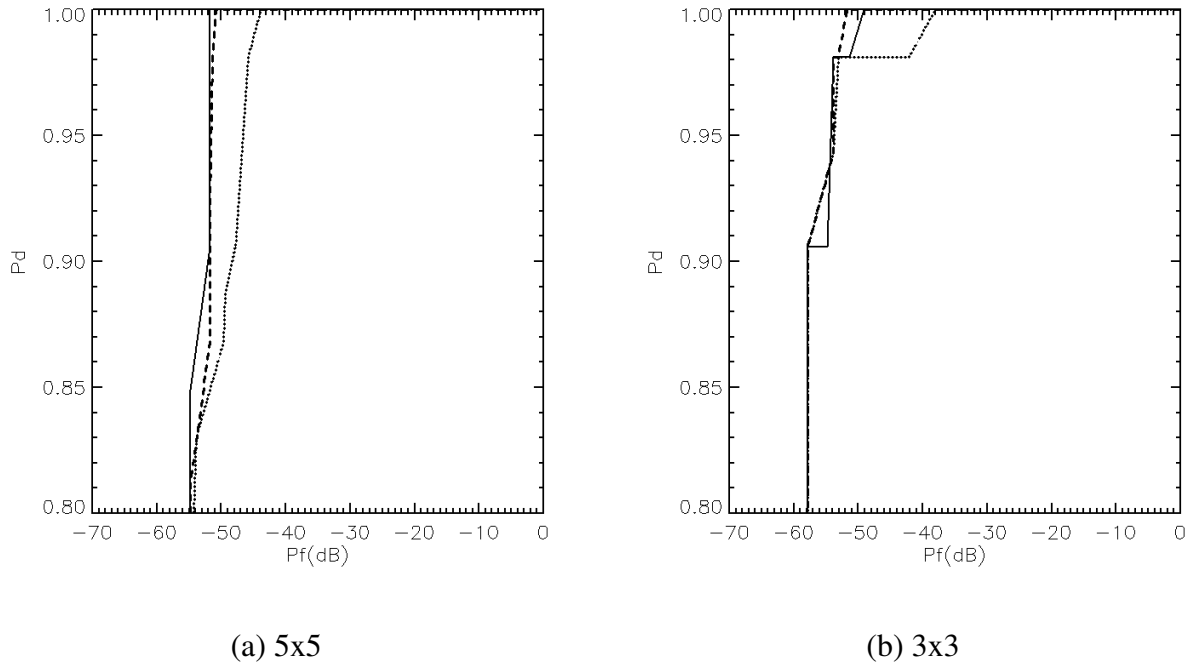


Fig. 11. ROC curves for GP-PNF fixing the target window to (a) 5x5 and (b) 3x3, varying the size of the training window. Solid line: $W_{tr} = 20$; Dashed line: $W_{tr} = 30$; Dotted line: $W_{tr} = 10$.

488 window 5x5 (after multi-looking) and training window 20x20 (this is the reason why these
 489 values were employed in this work). However, looking at these curves also the choice 3x3
 490 and training window 30x30 could be employed. Clearly, these results are strongly depen-
 491 dent on the resolution of the sensor and the dimensions of vessels of interest. Therefore,
 492 no definitive statement can be made and the windows' dimensions may change greatly if
 493 another detection task (e.g. with another satellite sensor) is attempted.

494

DISCUSSIONS

495 The aim of this section is to collect and discuss some of the results obtained in the
 496 manuscript.

497 From the comparison of two dual-polarimetric modes with the GP-PNF, it can be ob-
 498 served that HH/VV provides better performance than HH/HV (being almost as good as the

quad-pol version). Similar results were found comparing the different polarimetric modes exploiting other two ship detectors: the degree of polarization in Shirvany *et al.* [28] and the Generalized Likelihood Ratio in Liu *et.al* [22].

This may appear contradicting the fact that the best single channel for ship detection was demonstrated to be *HV* [23], [6]. An interpretation of these results is that the co-polarizations allow to characterize more precisely the sea polarimetric behavior and, therefore, to identify more accurately its complementary (target) subspace. Just as an example, exploiting only *HH/HV* it would not be possible to discriminate (from a polarimetric point of view) between Bragg scattering (often associated with the sea) and horizontal dihedral scattering (often associated with vessels).

Another remark could be made comparing the results presented in this paper with the ones recently obtained with RADARSAT-2 (where a ground survey was available) [44]. Exploiting RADARSAT-2 the GP-PNF was able to detect all the validated vessels in a dataset of four images (49/49). However, at this stage it is still not possible to come with some conclusive statement regarding the best frequency to exploit for ship detection, since the weather conditions, sensor resolution and typology of vessels are different in the dataset considered. Currently, work is in progress toward providing a fair comparison between different frequencies.

With the aim of testing the detector over a larger area and qualitatively compare the performance of different polarimetric modes, the GP-PNF was tested over the rest of the dataset. Please note, lacking of ground truth, it is not possible to provide any validation in this part of the dataset. The quad-pol gives the best detection performance narrowly followed by the *HH/VV* mode. However, *HH/HV* is able to detect at least two targets that can be retrieved with quad-pol (stressing the threshold) but not with *HH/VV*. This is a good indicator that all

523 the polarimetric information is important and even though the HH/VV mode could be a good
524 substitute of quad-pol for ship detection, still there may be situations where some vessels are
525 only detectable using quad-pol.

526 As a final remark, this paper wants to be a step in the process of thoroughly validating the
527 GP-PNF for L-band. In order to have a definitive statement regarding the behavior of the
528 detector (necessary for operational purposes) different sea states conditions and targets has
529 to be considered, needing a larger amount of data.

530 CONCLUSIONS

531 In this paper the validation of a ship detector, the Geometrical Perturbations Polarimetric
532 Notch Filter (GP-PNF) with ALOS-PALSAR data over the Tokyo Bay was presented. The
533 GP-PNF bases its detection rule on the polarimetric differences between ships and sea back-
534 ground. In details, a Null in the target polarimetric space is set in correspondence of the sea
535 signature rejecting it and detecting the rest. This paper presented a test of the GP-PNF for
536 the first time ever with L-band data.

537 The ALOS-PALSAR quad-polarimetric dataset was acquired over Tokyo Bay in Octo-
538 ber 2008 presenting a very large amount of vessels of opportunity for testing the detector.
539 Moreover, in one of the areas a video survey was carried out during the acquisition allow-
540 ing quantitative analysis. 38 vessels were visible in the ground survey and of these 22 were
541 detected by the quad-polarimetric GP-PNF. A visual inspection of the RGB image was per-
542 formed and only 21 vessels were visible. The missing vessels were mainly small fiber-glass
543 boats. Regarding false alarms, in the area observable by the camera no false alarms are
544 identifiable in the quad-pol GP-PNF mask.

545 In order to test the feasibility of dual-polarimetry for ship detection, the GP-PNF was

546 applied to HH/VV and HH/HV data. As a general trend, the detection capability decreases
547 going from quad-pol to dual-pol HH/VV and finally to dual-pol HH/HV. This result was
548 already observed in other studies. An explanation is that the sea and ships are relatively well
549 characterized in the subspace observed by HH/VV, while using only one co-polarization a
550 large portion of the information may be lost.

551 In order to compare the detection mask in a larger context of ship detection, other two
552 detectors were considered. The first exploits quad-polarimetric data and estimates the po-
553 larimetric entropy, the second employs single polarization data and performs a test on the
554 intensity of the S_{HV} channel setting the threshold with a Constant False Alarm (using a
555 K-distribution). The results show that the entropy detector has a good detection capabil-
556 ity missing only one target more than the GP-PNF (21 instead than 22 detections), but it
557 is strongly affected by false alarms where the level of the backscattering is low. On the
558 other hand, the S_{HV} has no problems with false alarms but has a limited detection capability
559 compared to quad-polarimetric detectors (18 instead than 22 detections).

560 Finally, the scene presents areas with seaweed farms. Also due to the low backscattering
561 of the areas, the entropy provides very good detection and outperforms the GP-PNF, when
562 the ordinary threshold is used (the quad-pol GP-PNF misses some of the wooden platforms.
563 The S_{HV} intensity does not identify any wooden platform.

564 As a final analysis the false alarms are investigated in an area of the dataset where no
565 vessels are expected. The results are then used in cooperation with the validated detection
566 masks to provide Receiver Operating Characteristics (ROC) curves for comparing different
567 detectors. It appears that the quad-pol GP-PNF provides the best characteristics, followed
568 by the HH/VV GP-PNF and the entropy detector. Interestingly, the results suggest that it is
569 possible to have a probability of detection approximately equal to one with a Probability of

570 False Alarm smaller than 10^{-5} .

571

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574

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